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Fraction Computation

2015-03-13

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Table of Contents

Click on a topic to go to that section.

- Adding Fractions with Common Denominators
- Adding Mixed Numbers with Common Denominators
- Subtracting Fractions with Common
 Denominators
- Subtracting Mixed Numbers with Common
 Denominators
- Multiplying Fractions and Whole Numbers

Adding Fractions with Common Denominators

Return to Table of Contents

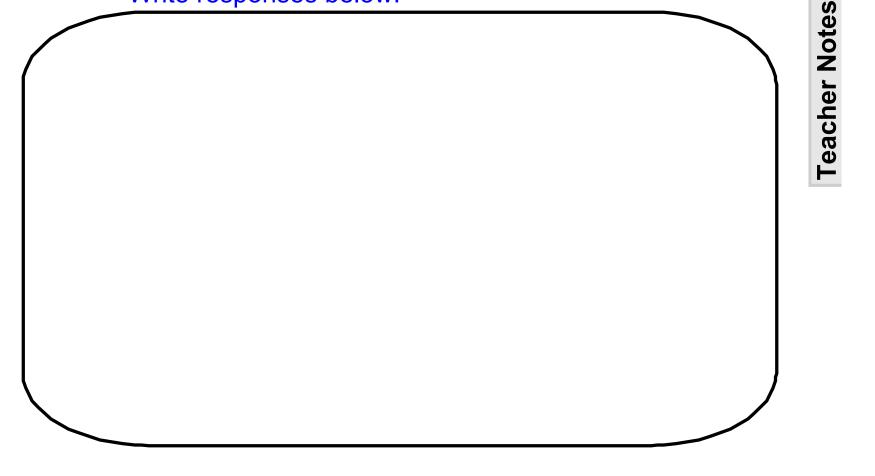


For this section you will need to prepare cut strips of paper for each student in your class. They need to be long enough to divide into 3rds and then 6ths.

> Return to Table of Contents

What are the important concepts we need to remember about fractions?

Write responses below:



What are the ways we can write or visualize fractions?

Remember fractions can be written:

- 1. By writing words for the fractional parts
- 2. Drawing a picture, such as a circle or square showing equal parts
- 3. Writing an equation or number sentence
- 4. Representing the fractional parts on a number line

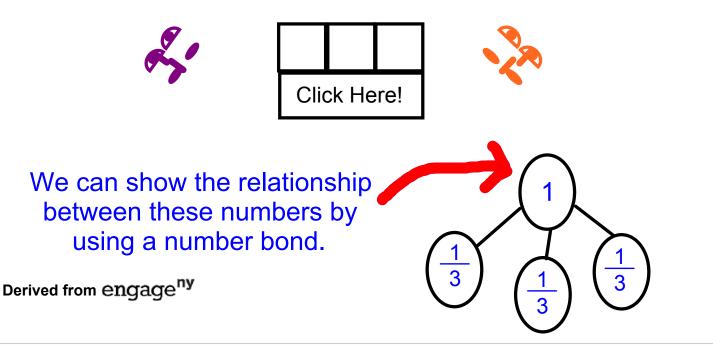
We will use all of these different ways as we learn how to add fractions with common denominators!

Adding Parts to Make a Whole

Take out one strip of paper you were given. This paper represents a whole. How can you divide this strip into 3 equal parts?

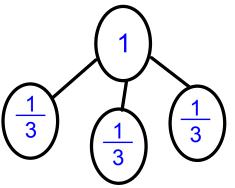
Fold the paper into equal parts and draw lines on the creases.

What is each section now representing?



Number Bonds

Number bonds are a tool you can use to show how a WHOLE is broken into parts. The numbers are "bonded" to the whole (or number 1) to show how all the individual parts together equal 1. By using a number bond, you can easily see how the "parts" added together equal the whole. You can use this to compose an addition sentence with fractions.



If we know that our strip is equal to one whole. Can we write an addition sentence showing how our thirds add up to one whole? How?



Continued...

When you take a part a whole, it is called decomposing. Previously, we decomposed our whole strip of paper into thirds. We discovered 1/3 is the unit fraction and you can add those thirds together to compose, or make, the whole. A number bond helps us see how the fractions are related to each other when creating an equation.

When we write the addition sentence, we are creating an algebraic equation using fractions...

$$1 = \frac{1}{3} + \frac{1}{3} + \frac{1}{3}$$

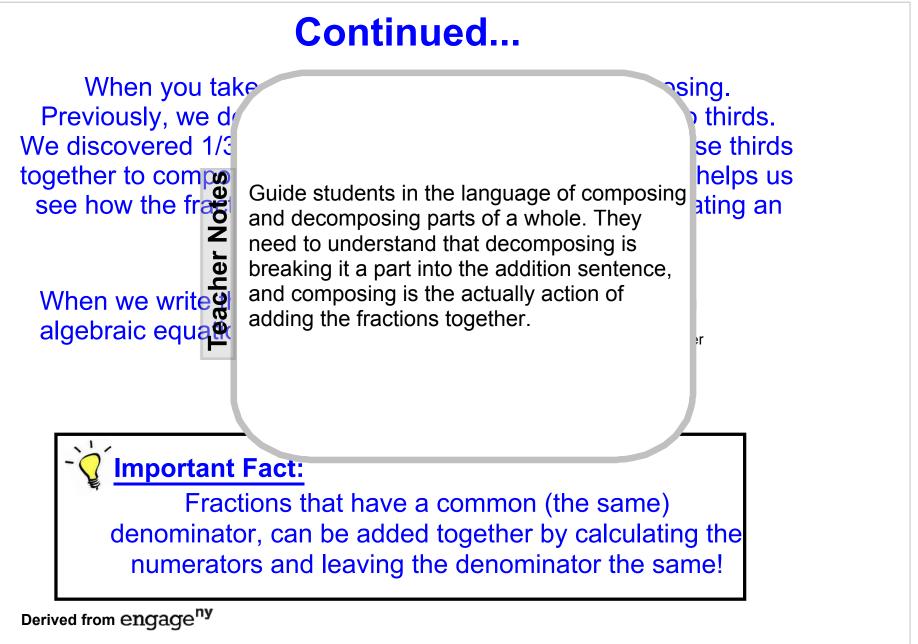


Important Fact:

Fractions that have a common (the same) denominator, can be added together by calculating the numerators and leaving the denominator the same!

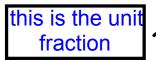
Derived from engage^{ny}

Slide 9 (Answer) / 110

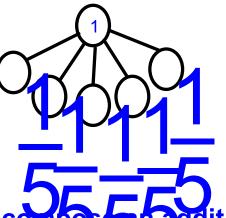




Look at the tape diagram below. What is the unit fraction?



...because the unit fraction represents the rumber of pieces the whole has been divided into. It always has the number 1 in the numerator.

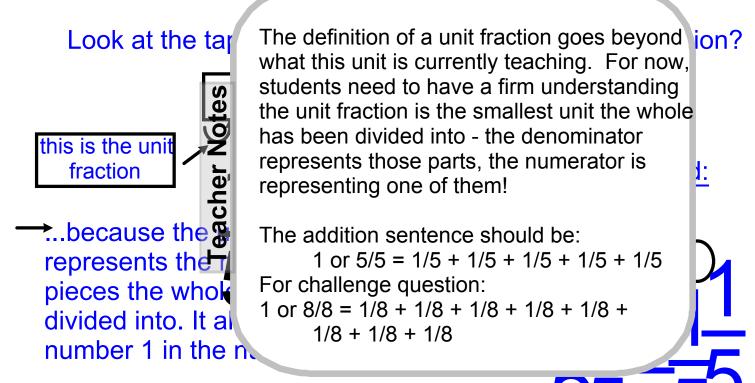


Number Bond:

Look at the number bond. How can we compose an addition sentence to equal the shaded parts using our unit fraction?

★ How could you write an addition sentence if a whole was composed of 8 equal parts? Use a tape diagram to show your work.

Finding the Unit Erection



Look at the number bond. How can we compose an addition sentence to equal the shaded parts using our unit fraction?

★ How could you write an addition sentence if a whole was composed of 8 equal parts? Use a tape diagram to show your work.

Regrouping Fractions with Common Denominators

Let's look at composing fractions another way:	$1 = \frac{1}{3} + \frac{1}{3} + \frac{1}{3}$
If we add parenthesis	$1 = \left(\frac{1}{3} + \frac{1}{3}\right) + \frac{1}{3}$
Can we say \longrightarrow	$1 = \frac{2}{3} + \frac{1}{3}$
	. We rearouned the frac

Yes!

We regrouped the fractions to add them in a different way but the answer is still the same!

Regrouping Fractions with Common Denominators

For a quick review!

Do you remember our properties of addition? What property is being represented when we added the parenthesis?

A. Commutative PropertyB. Associative Property

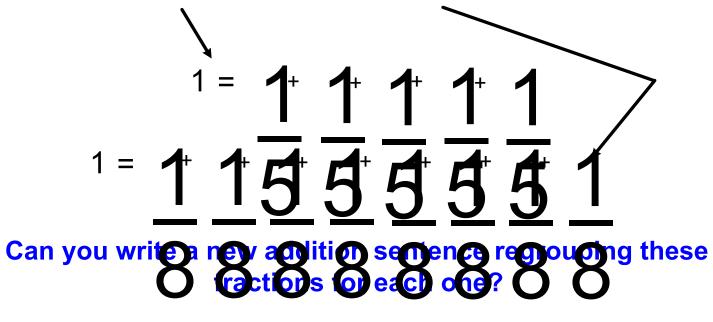
C. Distributive Property

Click for answer

Remember, fractions with a common denominator, can be added together. Calculate the numerators and leave the denominators the same!



Previously, we wrote addition sentences for a whole made up of 5 equal parts and 8 equal parts (two slides ago).



How are your answers different from others around you?

Are the different regrouping equations still correct?



Let's double the units of our whole. Fold your strip of paper on the creases and then fold it one more time in half. Open it up.

How many pieces are in our strip now? What is the unit fraction?

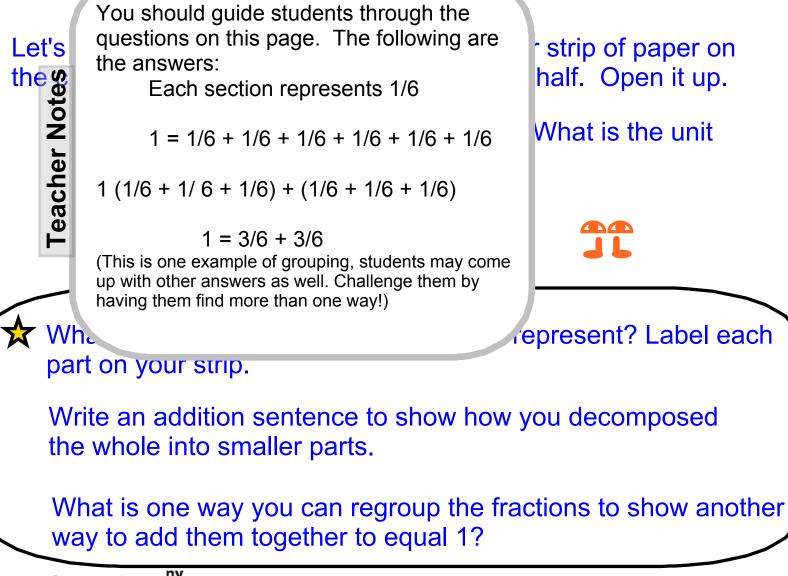


What does each unit section of the strip represent? Label each part on your strip.

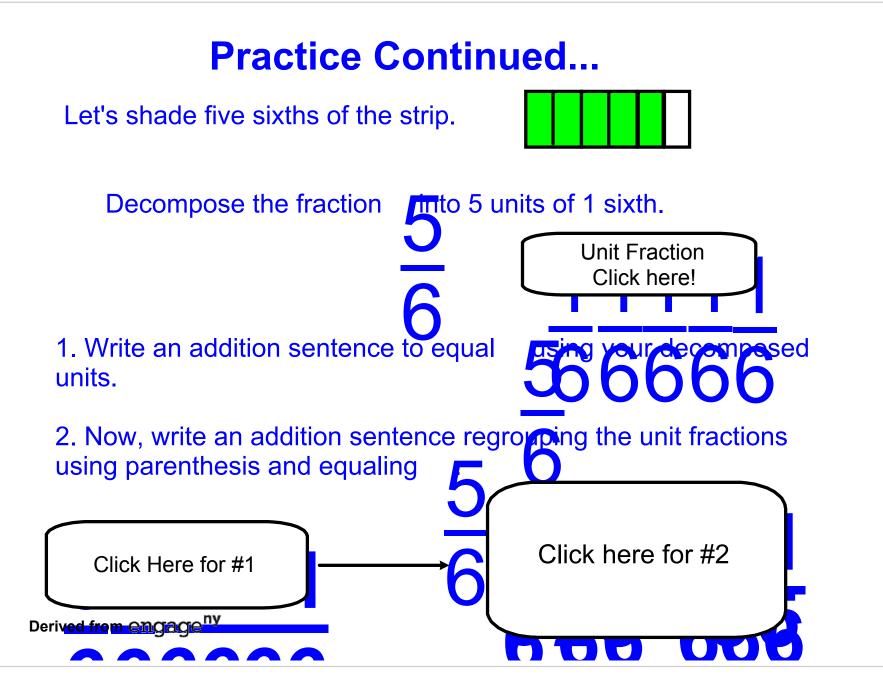
Write an addition sentence to show how you decomposed the whole into smaller parts.

What is one way you can regroup the fractions to show another way to add them together to equal 1?

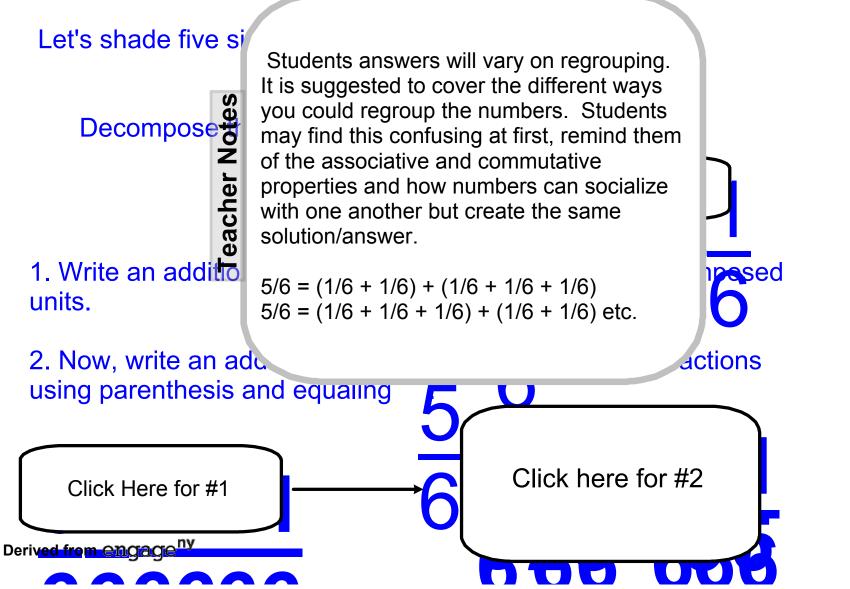
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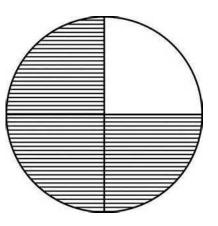
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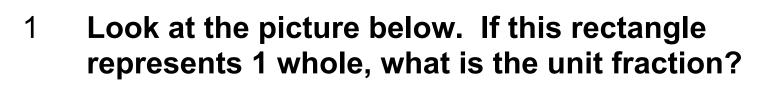


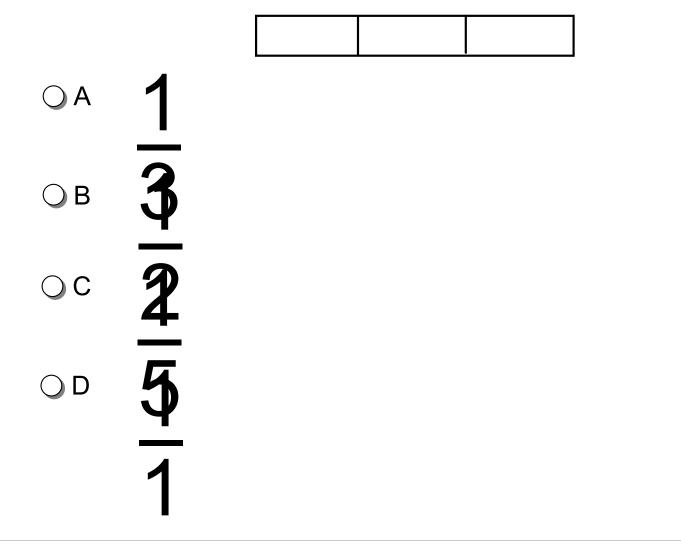


With a partner complete the following:

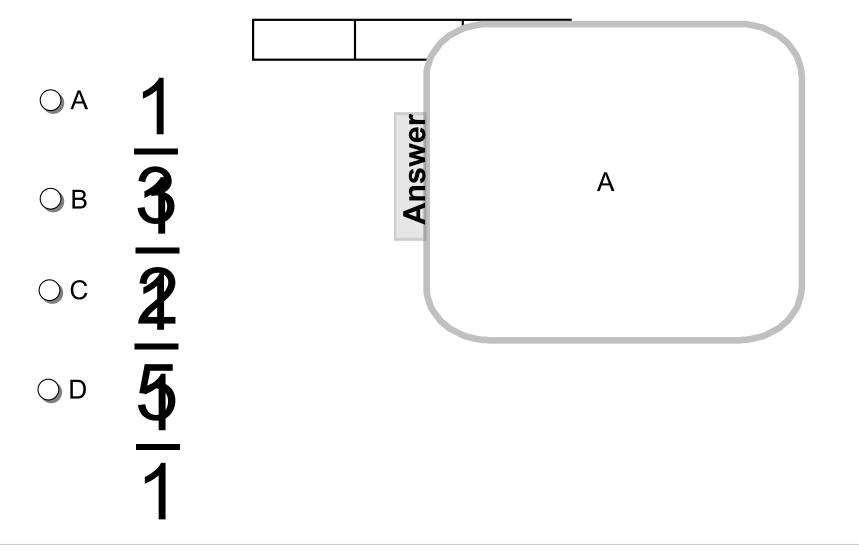


- 1. Copy this shape then identify how many parts are shaded in the circle
- 2. What is the unit fraction? Write an addition sentence using the unit fraction to equal the shaded parts.
- 3. How can you regroup the fractions to make a new addition sentence equaling 3 fourths?
- 4. Complete: 3 2 ?









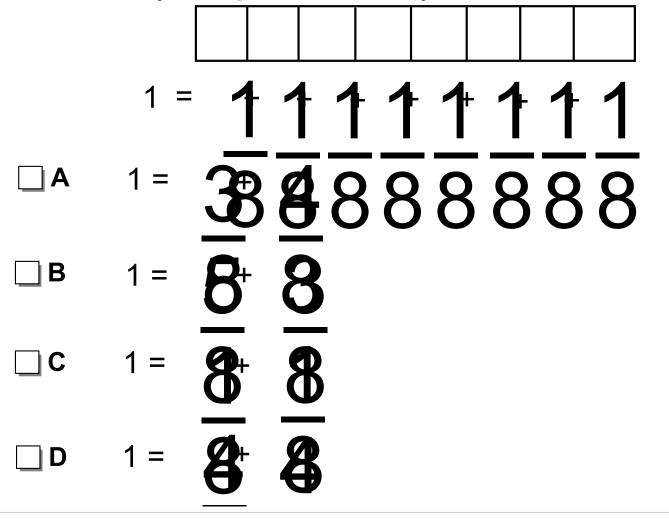
2 The rectangle represents one whole. Based on the units within this picture, which of the following addition equations shows how you can decompose the whole.

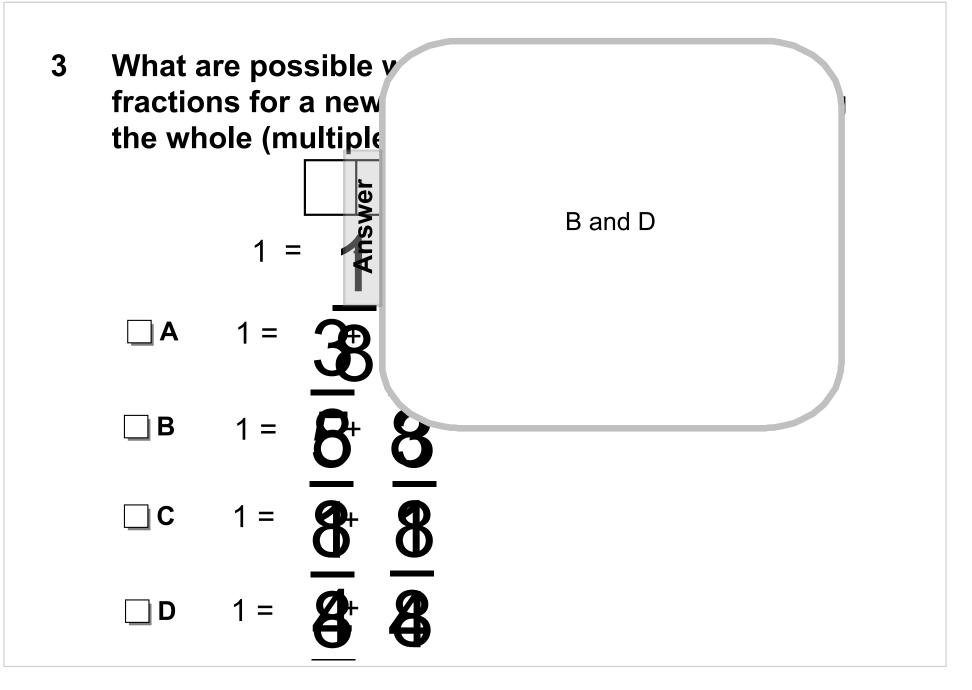
$$\bigcirc A \ 1 = 1$$

$$\begin{array}{c} \circ & 1 = \\ 2 \\ 1 = \\ 3 \\ \hline 3$$

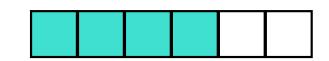
2 The rectangle represents one whole. Based on the units within this pict addition equations decompose the wh Answei С = В $\bigcirc \mathbf{C}$ 888888 D OE 5 =

3 What are possible ways you can regroup these fractions for a new addition sentence still equaling the whole (multiple answers!)?



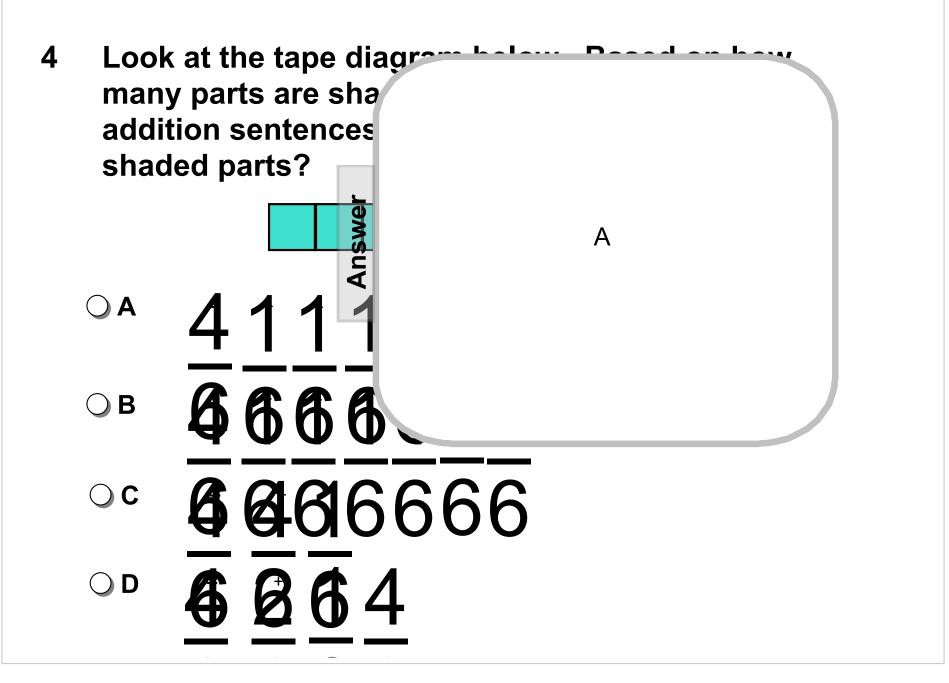


4 Look at the tape diagram below. Based on how many parts are shaded, which of the following addition sentences correctly decomposes the shaded parts?



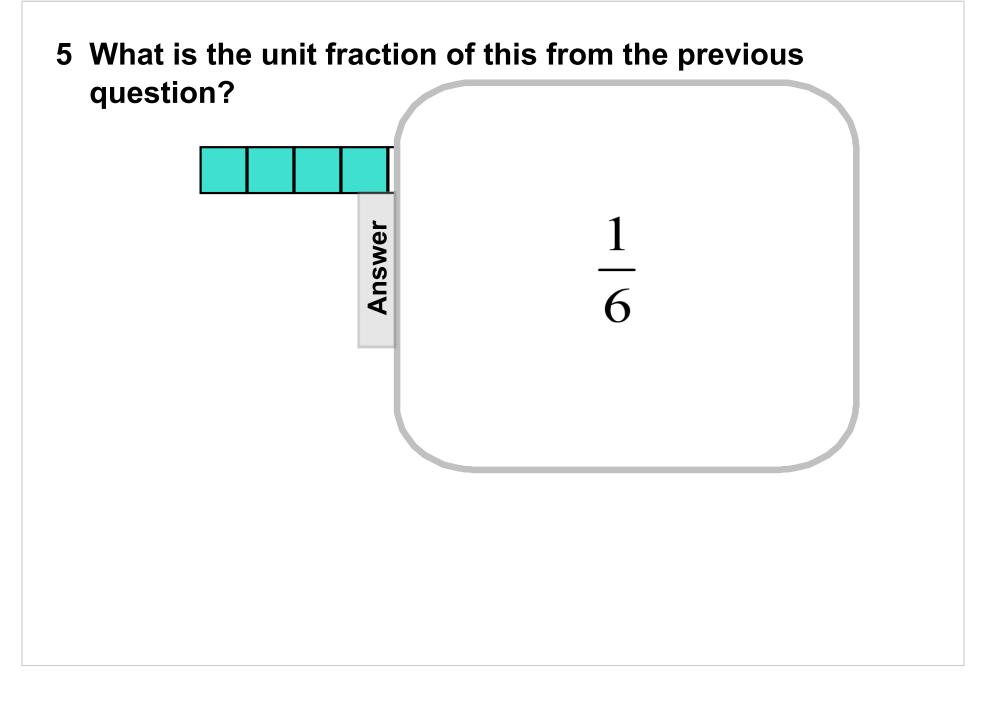
▲ 41111
● 46666611
● 66666666

 $\bigcirc \mathbf{D}$



5 What is the unit fraction of this from the previous question?

	-		

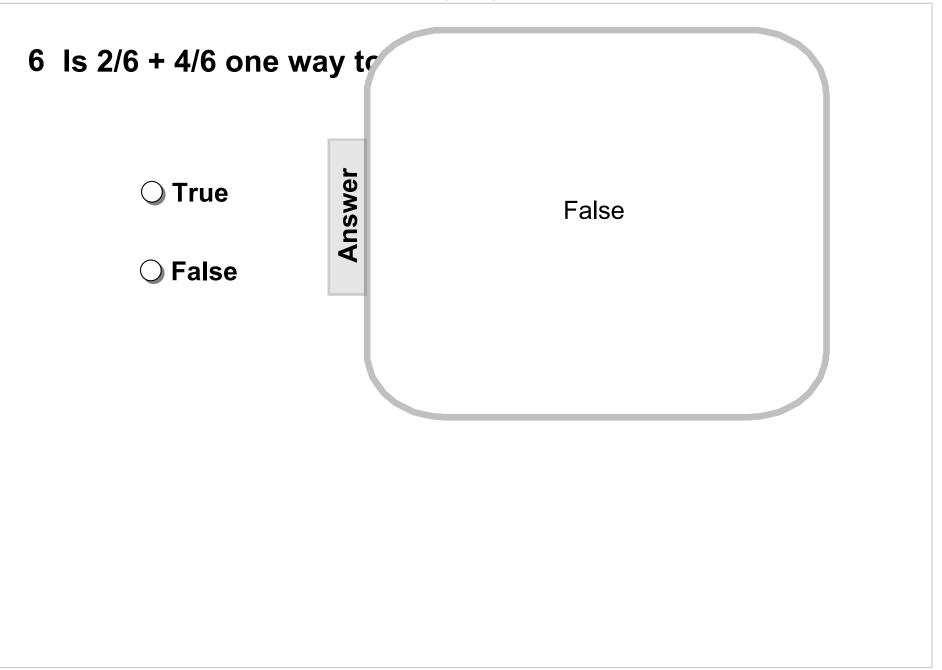


6 Is 2/6 + 4/6 one way to regroup

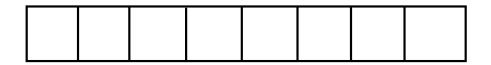
◯ True

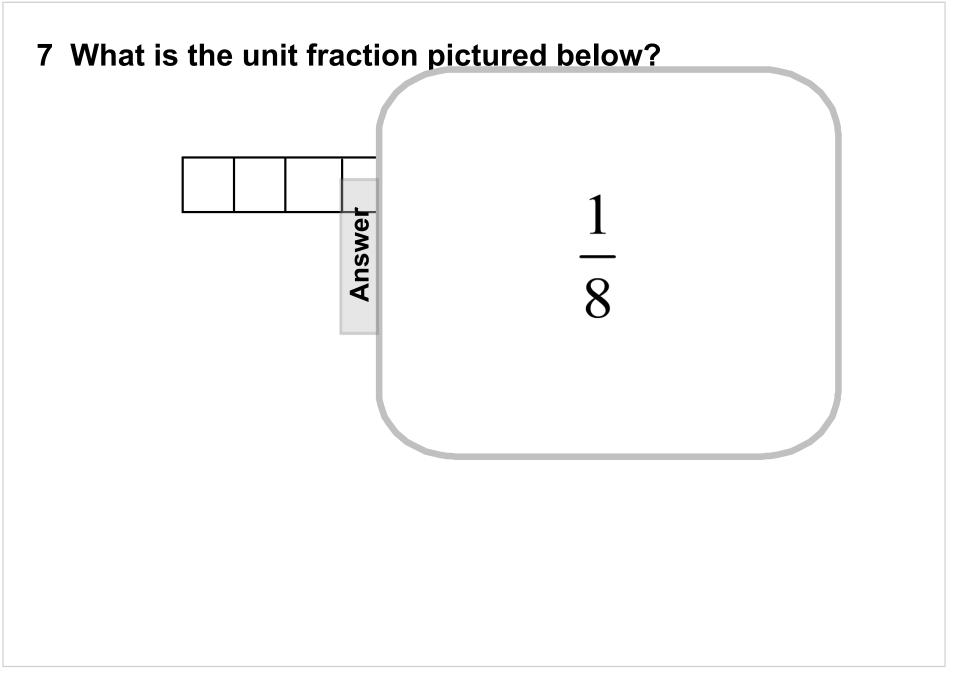
1111 6666

 \bigcirc False



7 What is the unit fraction pictured below?

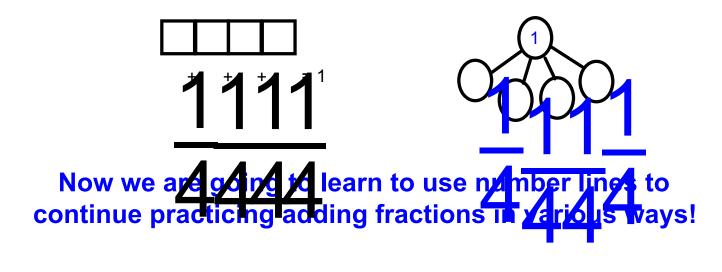




Visuals are Vital

Being able to create a picture with fractions is important, not only for your own understanding but so you can also show your work on assignments and tests!

So far we have used the tape diagram and number bonds to visualize how to decompose, compose (add) fractions.



Adding Fractions on a Number Line

In the previous unit, you learned how to count and label fractions on a number line.

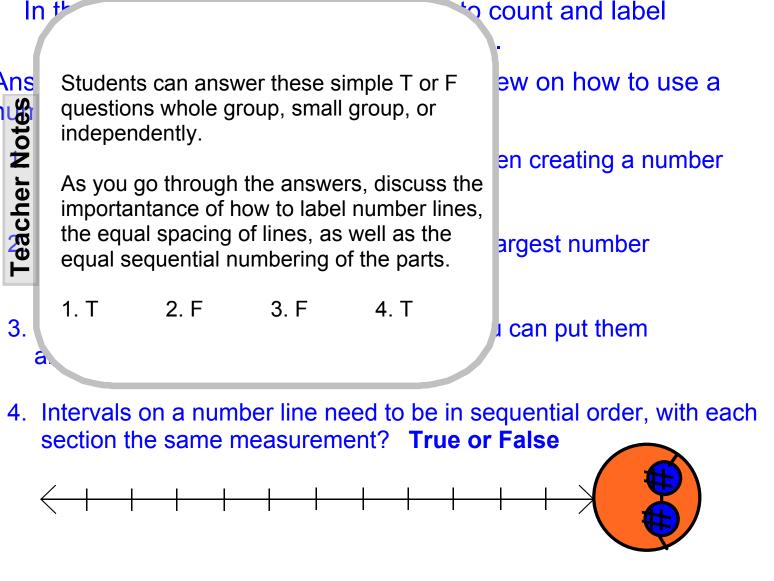
Answer the questions below for a quick review on how to use a number line.

- 1. The intervals have to be equally spaced when creating a number line. **True or False**
- 2. You label the number line starting with the largest number first. **True or False**
- 3. When placing points on the number line you can put them anywhere you want. **True or False**

4. Intervals on a number line need to be in sequential order, with each section the same measurement? **True or False**

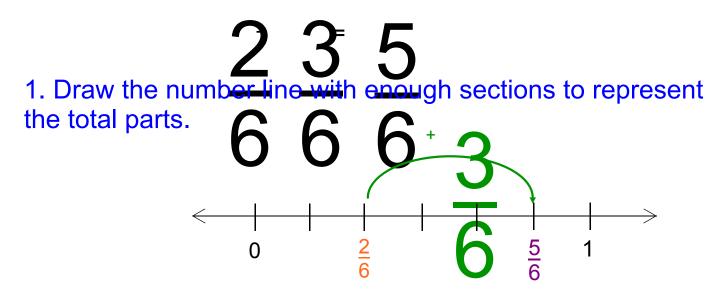
Adding Fractions on a Number Line

to count and label



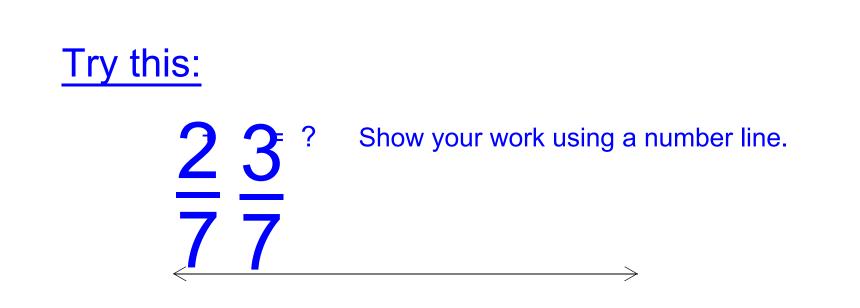
The Number Line in Action

The number line is another way we can show our work when adding fractions.



2. Put your finger on two sixths.

- 3. Add the 3 sixths, counting one sixth, two sixths, three sixths
- 4. You can SEE how two sixths plus three sixths equals five sixths on the number line!



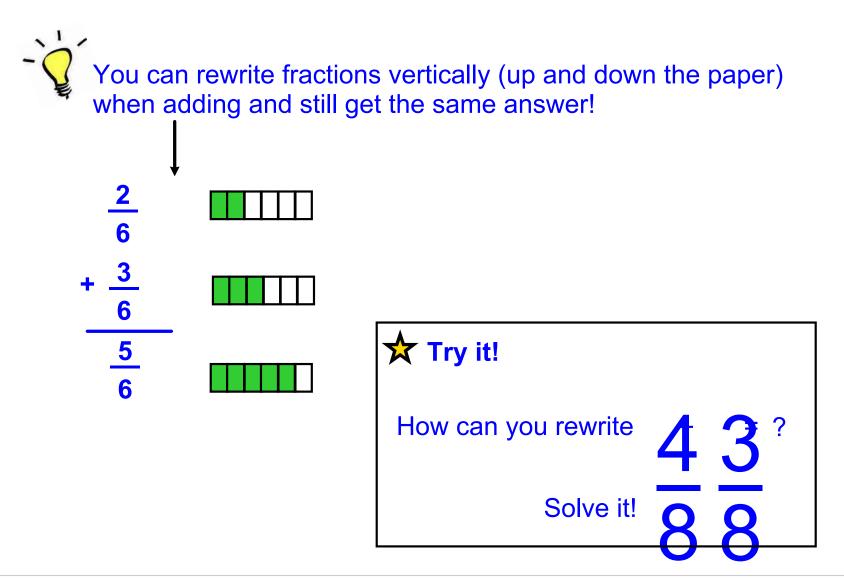
Do you prefer to draw tape diagrams or use number lines to show your work with fractions?

Slide 28 (Answer) / 110

Slide 29 (Answer) / 110

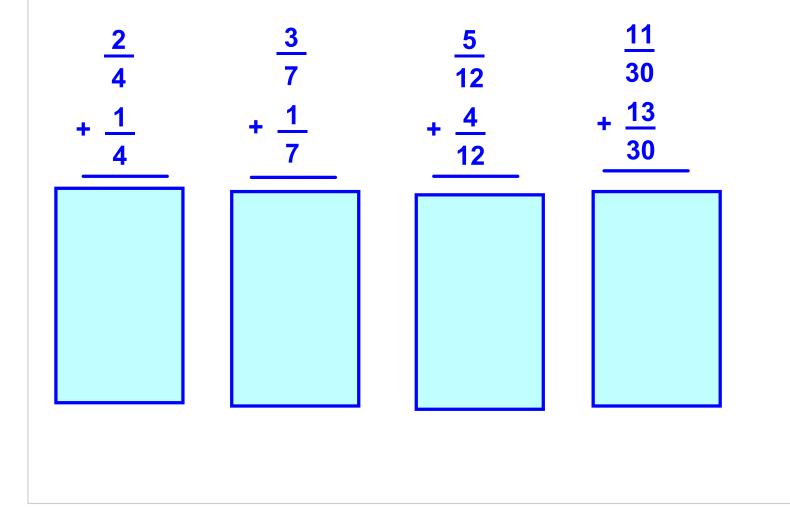
Slide 30 (Answer) / 110

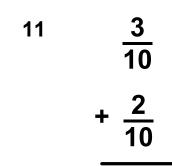




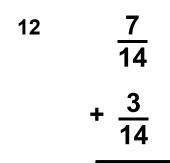
Try these!

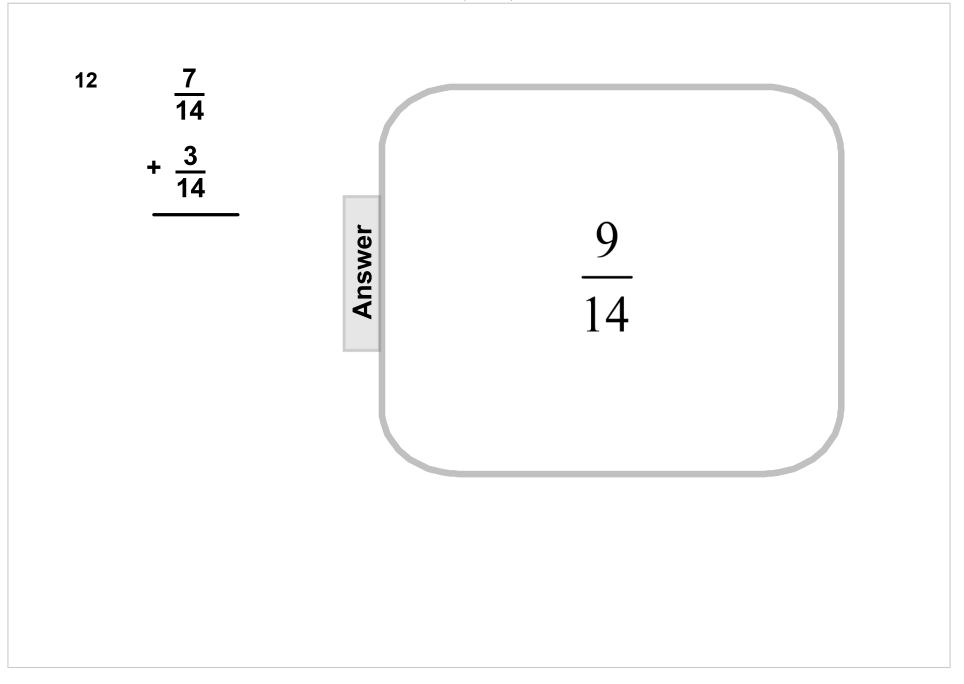
Click the boxes to see work and answers. Be sure to simplify all answers.



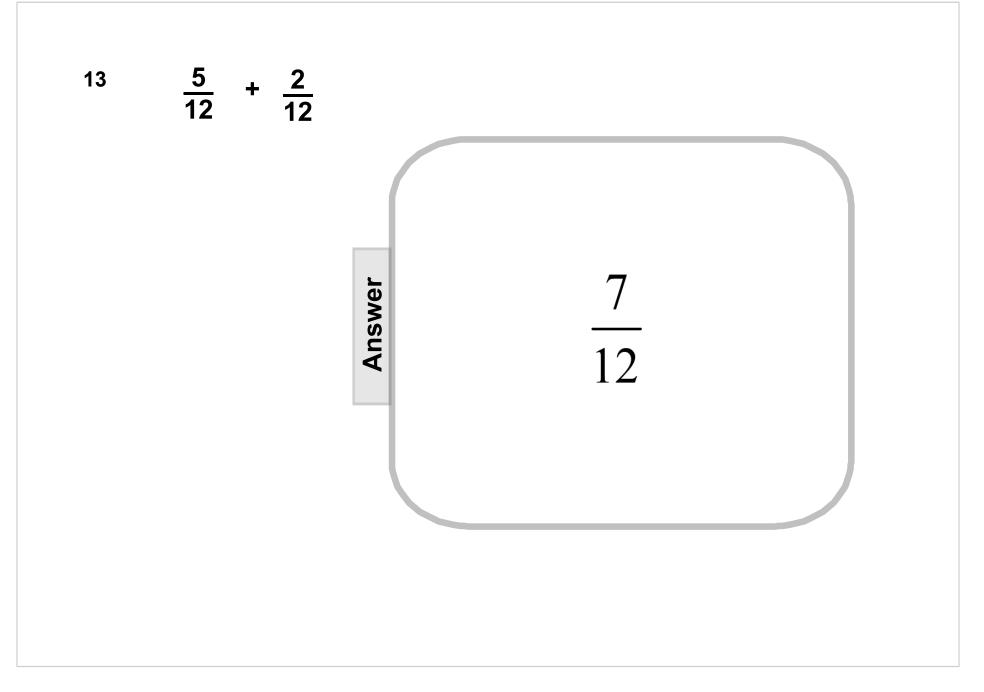


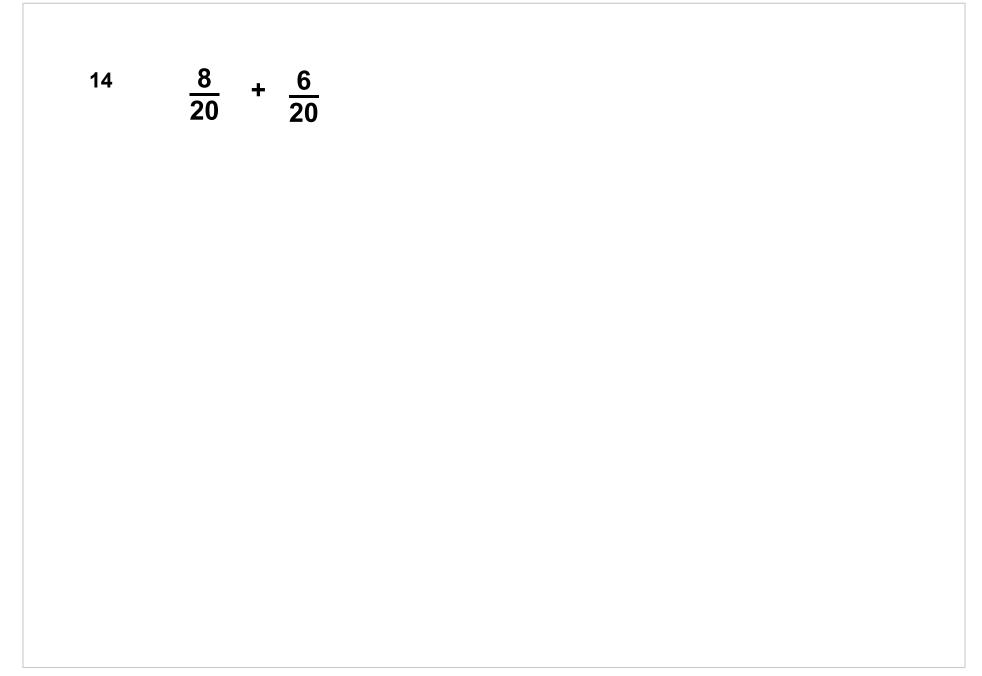
Slide 33 (Answer) / 110

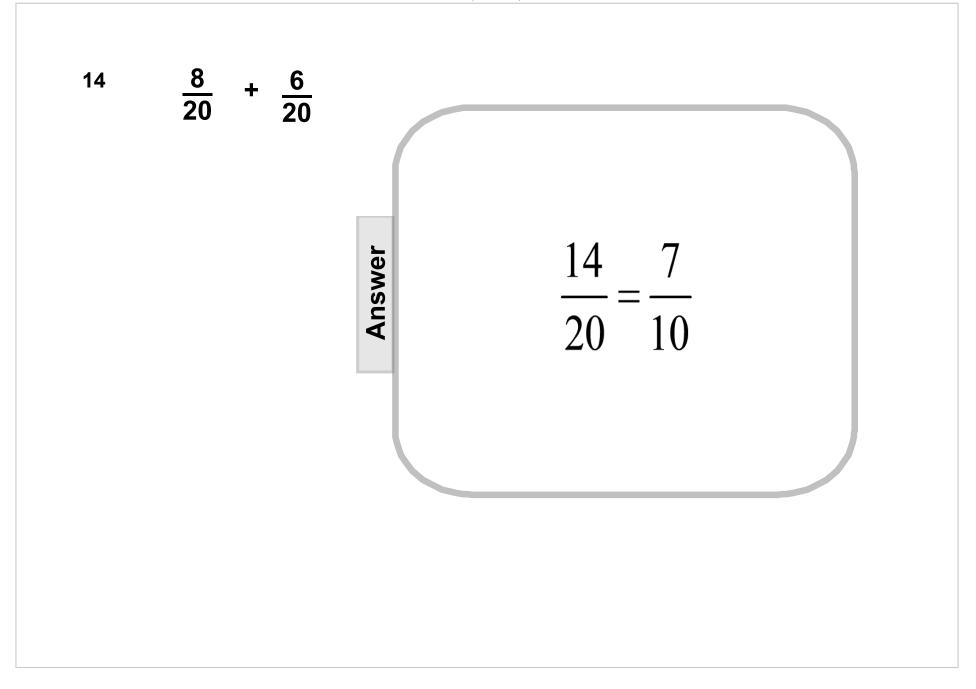




 $\frac{5}{12}$ + $\frac{2}{12}$ 13







Kaylee the Key to is here to help solve fraction word problems!

The K.E.Y.S. to Problem Solving

- K: Know the important information in the problem. Read the problem (more than once) and first find the main idea. (MAIN IDEA = What is the problem asking you to find?) Find all the important information that supports the main idea.
- E: Equation (or equations) is created to plan your strategy and organize the important information. Use equations to develop a strategy (i.e. algorithm, diagram). Strategy must be organized and easy to follow.
- Y: Yes, I have checked over my strategy and my answer is reasonable (makes sense). Use an estimate to check if your answer is reasonable.

S

S: <u>Solution is written in a complete sentence with the</u> correct label.

¹⁵ Lisa poured one-fifth of a bucket of water into a plastic wading pool. A few minutes later she poured 3/5 of a bucket into the wading pool. How much water did Lisa pour into the pool?

5

¹⁵ Lisa poured one-fifth of a bucket of water into a plastic wading pool. A few minutes later she poured 3/5 of a bucket much water did Lisa

Answer

¹⁶ Of the shirts in John's closet, 1/8 are green and another 5/8 are purple. What fraction of the shirts are green and purple? Slide 39 (Answer) / 110

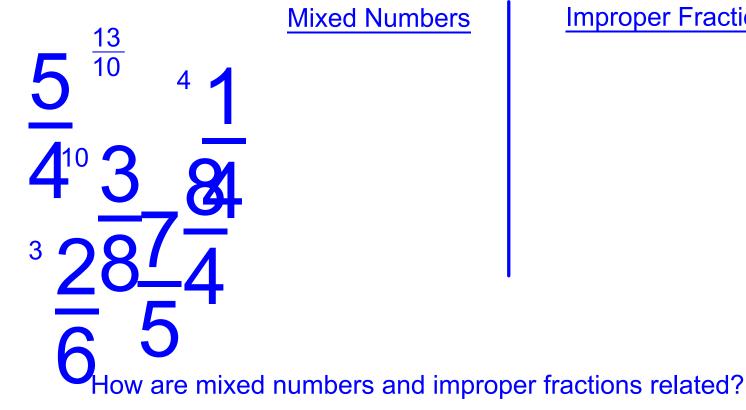
17 An athlete drank one-third of a bottle of sports drink in the beginning of a tennis match and another 1/3 of a bottle at the end of the tennis match. How much did she drink in all? Slide 40 (Answer) / 110

Adding Mixed Numbers with Common Denominators

> Return to Table of Contents

Improper Fractions and Mixed Numbers Review

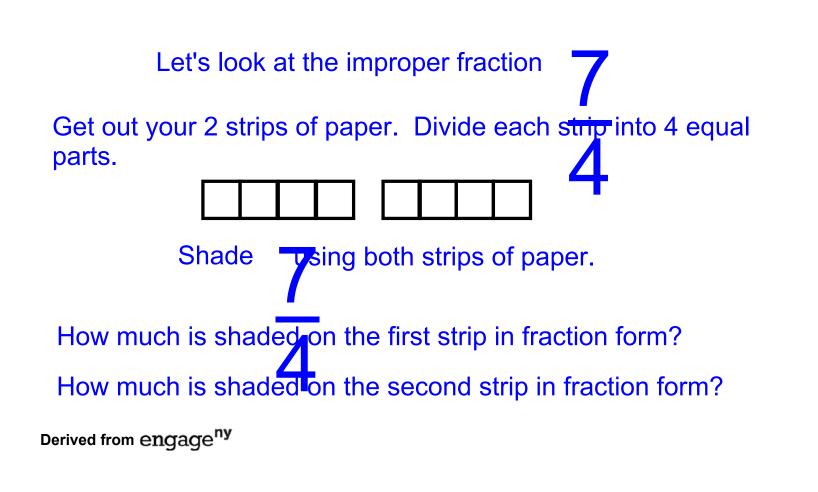
Place each number in the appropriate column.



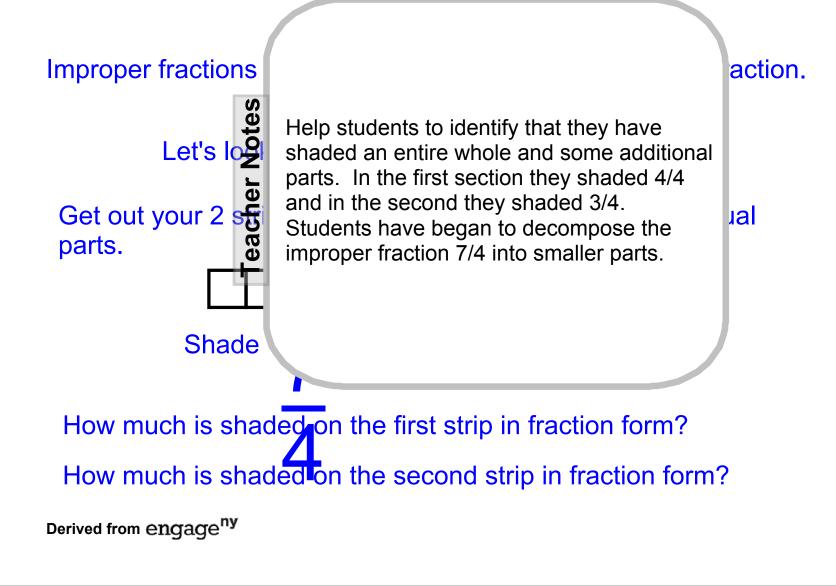
Improper Fractions

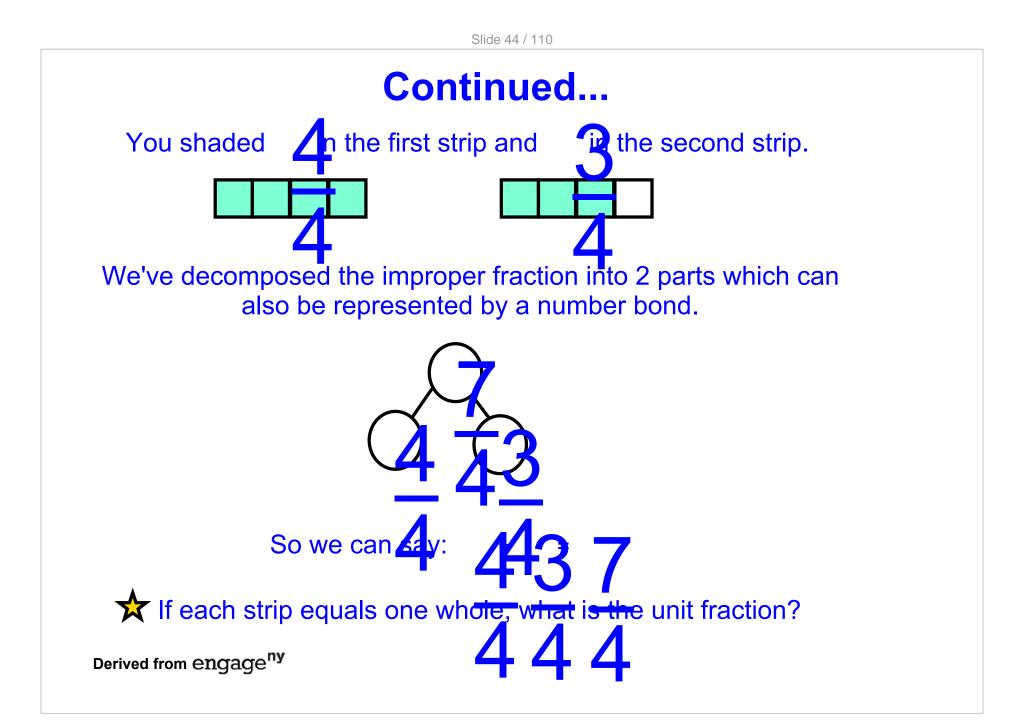
Decomposing Improper Fractions

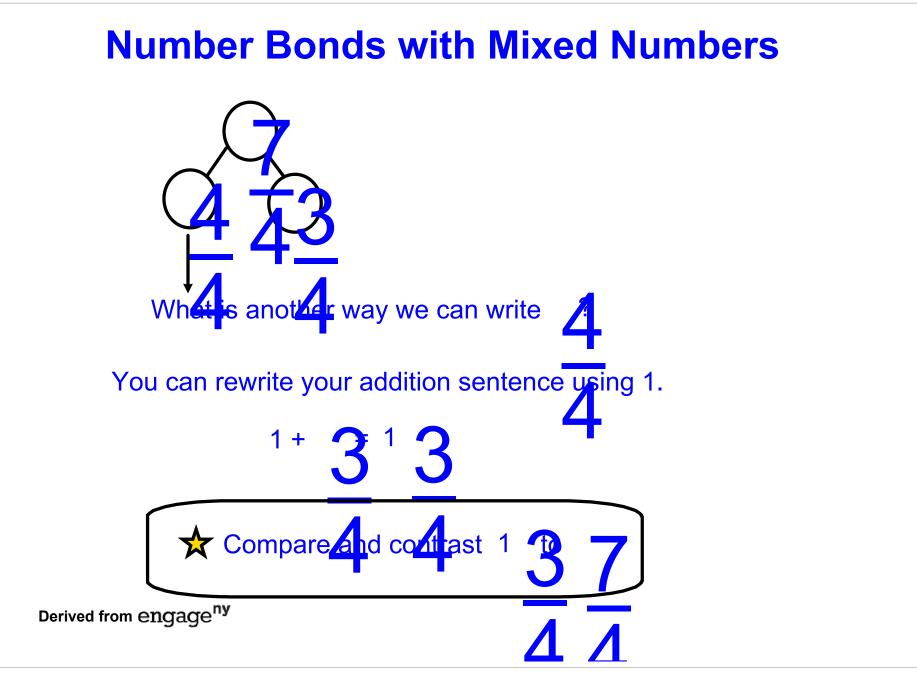
Improper fractions can be decomposed just like a regular fraction.



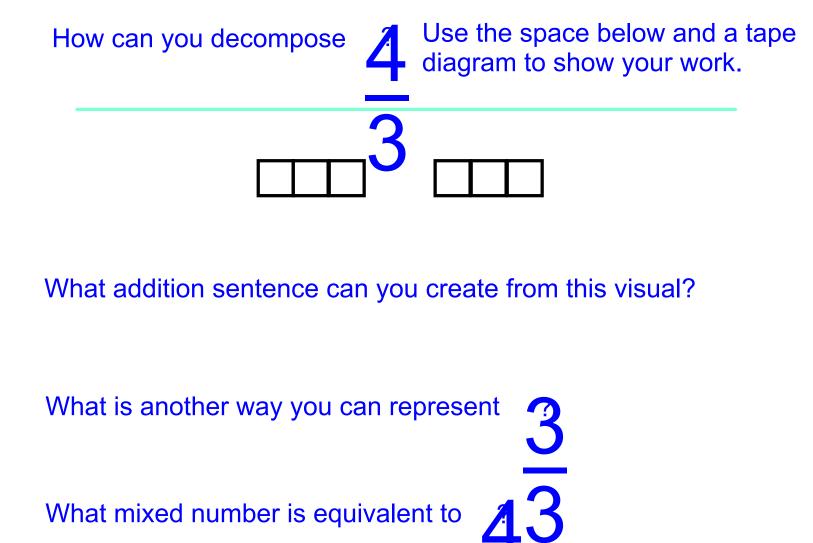








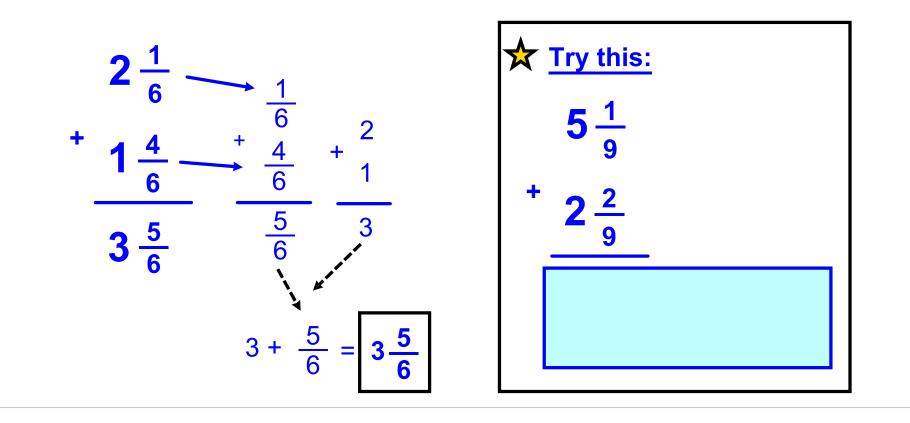
Practice Decomposing Improper Fractions

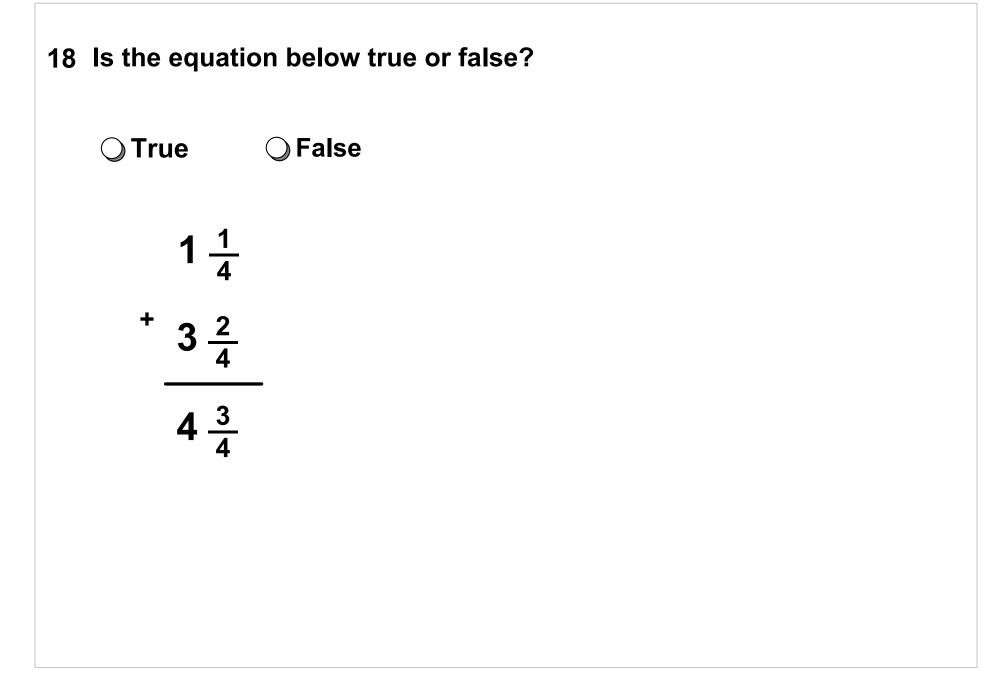


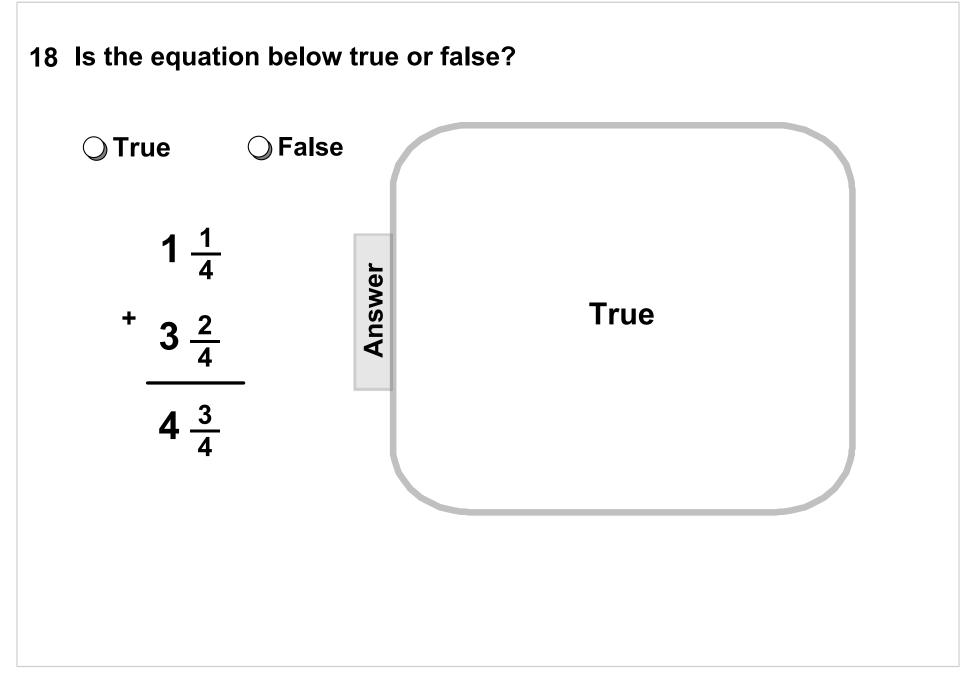
What mixed number is equivalent to

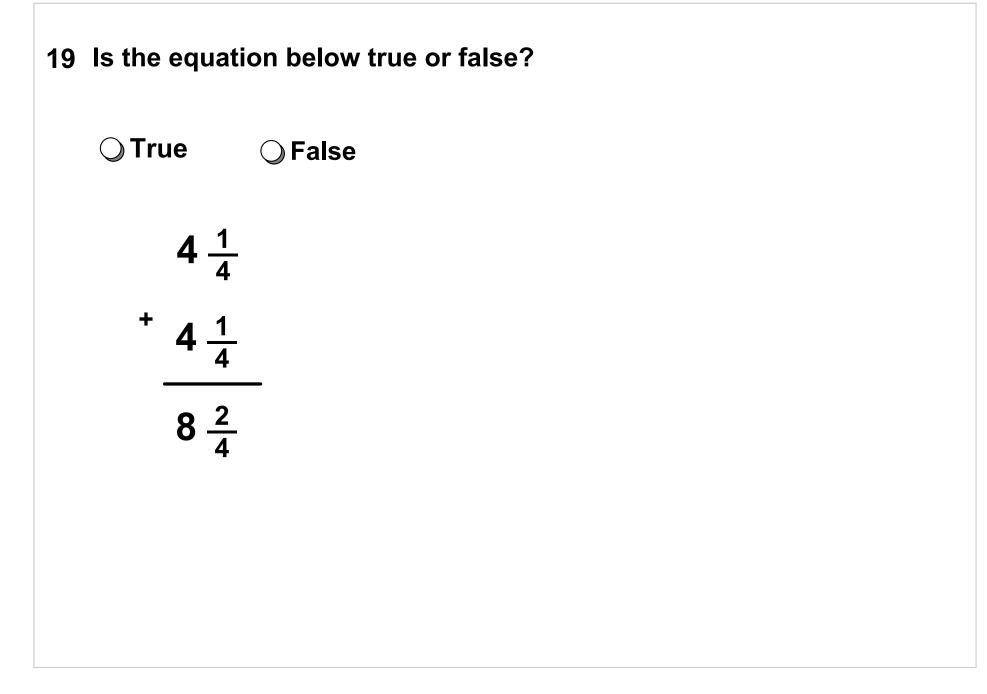
Adding Mixed Numbers with Common Denominators

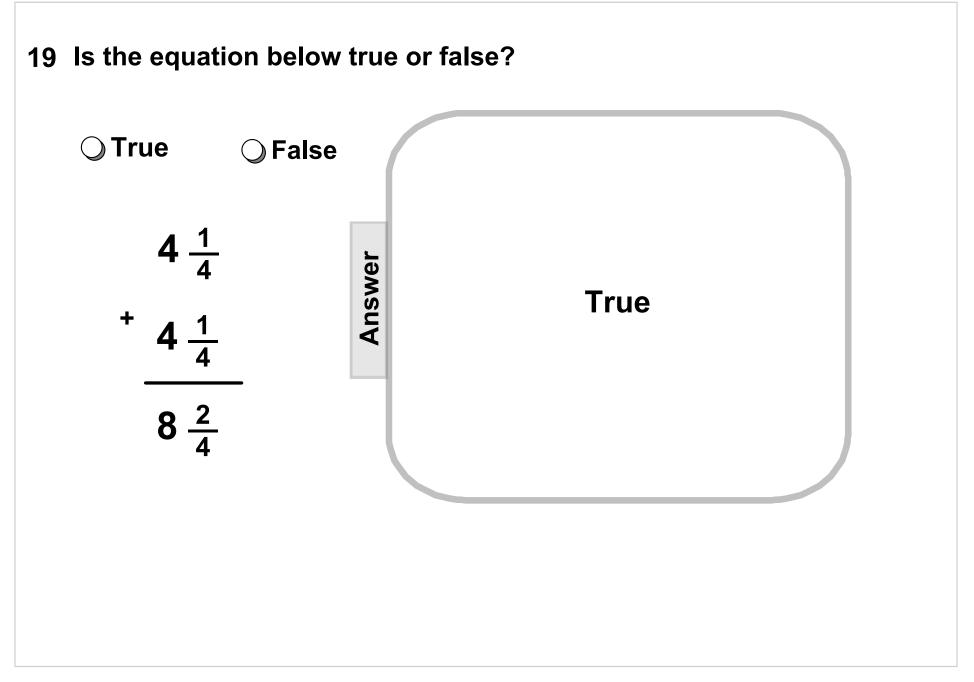
To add mixed numbers with common denominators, add the fractions then add the whole numbers. Make sure your answer is in simplest form.



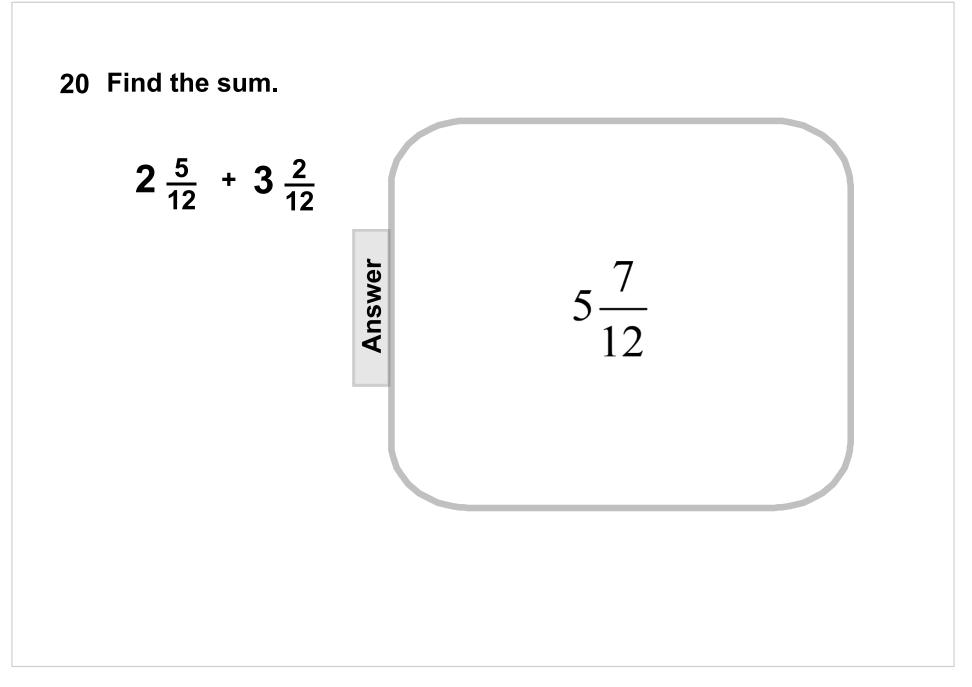




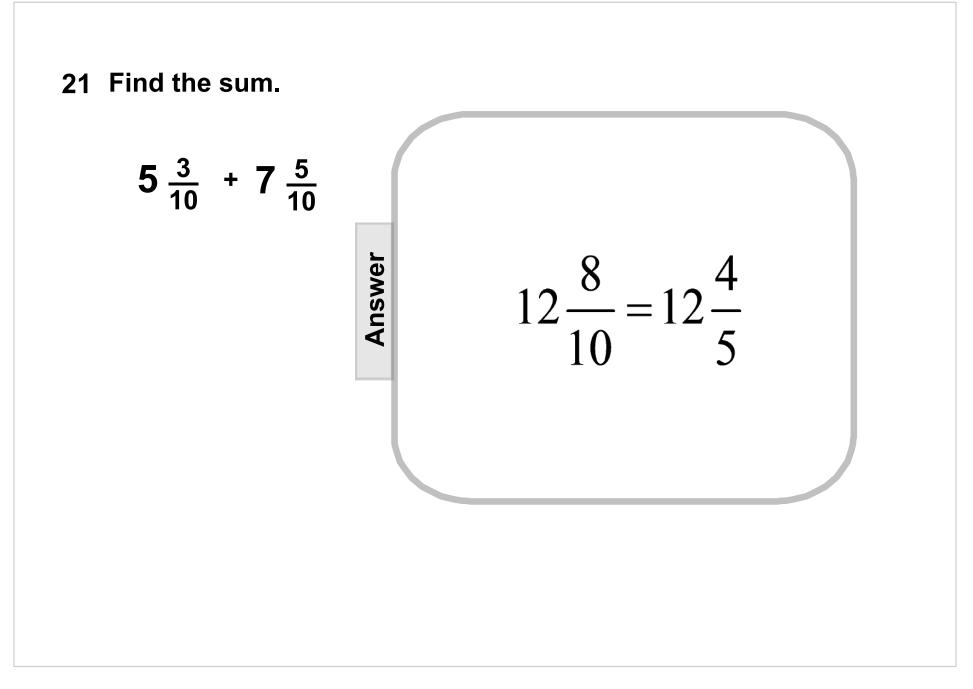




$$2\frac{5}{12} + 3\frac{2}{12}$$

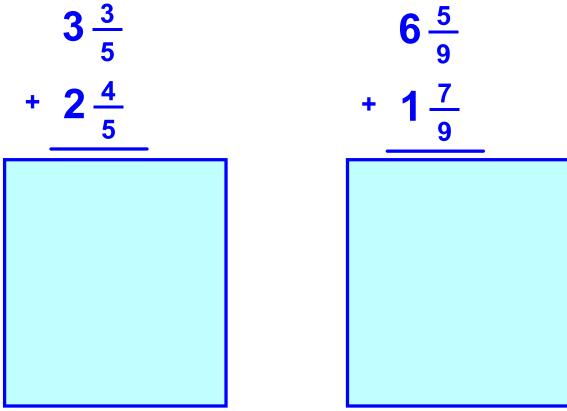


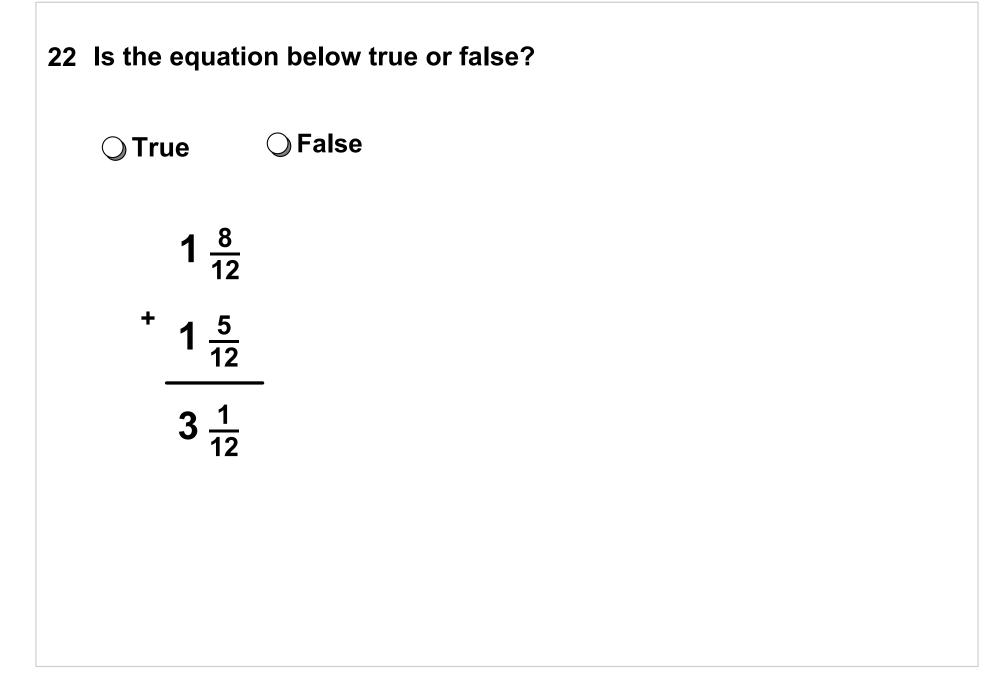
$$5\frac{3}{10}$$
 + $7\frac{5}{10}$

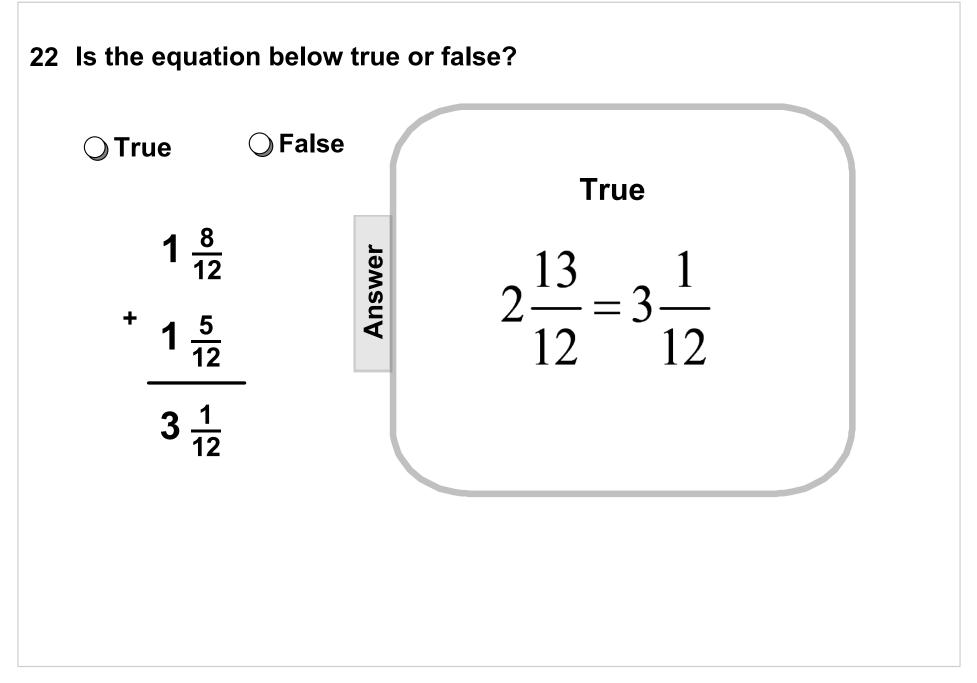


Adding Mixed Numbers with Common Denominators

Sometimes after you add the mixed numbers, the fraction is improper. When this occurs, you must rename the improper fraction as a mixed number and add it to the whole number.

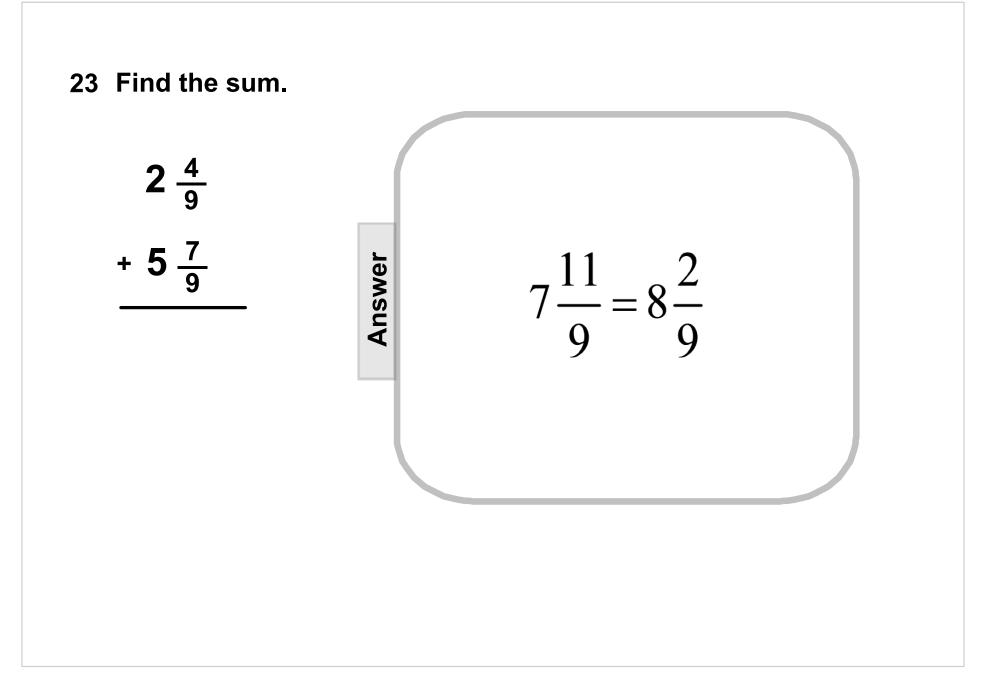




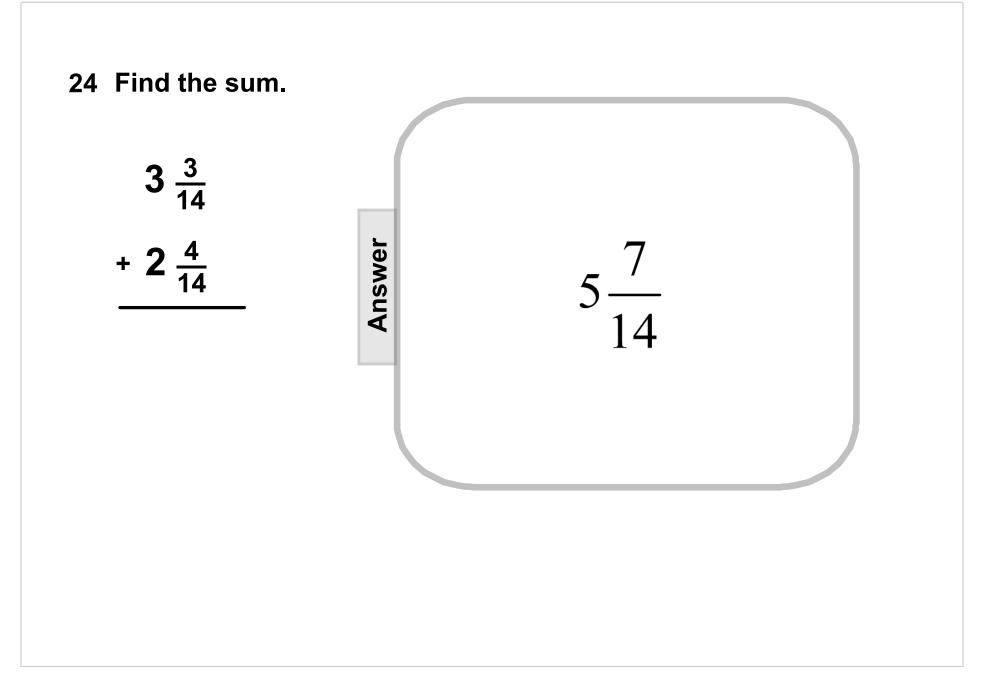


$$2\frac{4}{9}$$

+ $5\frac{7}{9}$



 $3 \frac{3}{14}$ + $2 \frac{4}{14}$



$$4\frac{5}{8} + 2\frac{3}{8}$$

-

Slide 56 (Answer) / 110

26 Madison's school is having a fun run during gym class. How many total miles did she run during weeks 4 and 5?

Week	Miles
Week 1	$2\frac{3}{5}$
Week 2	$1\frac{4}{5}$
Week 3	$2\frac{1}{5}$
Week 4	$3\frac{4}{5}$
Week 5	$1\frac{2}{5}$

Answer

27 Madison's school is having a fun run during gym class. How many total miles did she run during weeks 2 and 3?

Week	Miles
Week 1	$2\frac{3}{5}$
Week 2	$1\frac{4}{5}$
Week 3	$2\frac{1}{5}$
Week 4	$3\frac{4}{5}$
Week 5	$1\frac{2}{5}$

Answer

28 Madison's school is having a fun run during gym class. How many total miles did she run during the whole five weeks?

Week	Miles
Week 1	$2\frac{3}{5}$
Week 2	$1\frac{4}{5}$
Week 3	$2\frac{1}{5}$
Week 4	$3\frac{4}{5}$
Week 5	$1\frac{2}{5}$

Answer

Subtracting Fractions with Common Denominators

Return to Table of Contents

What are the ways we can write or visualize fractions?

Remember fractions can be written:

- 1. By writing words for the fractional parts
- 2. Drawing a picture, such as a tape diagram or circle
- 3. Writing an equation
- 4. Representing the fractional parts on a number line

We will use all of these different ways as we learn how to subtract fractions with common denominators!

Subtraction with Fractions

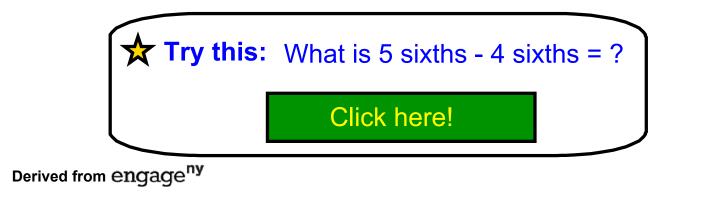
Let's practice a few basic subtraction problems:

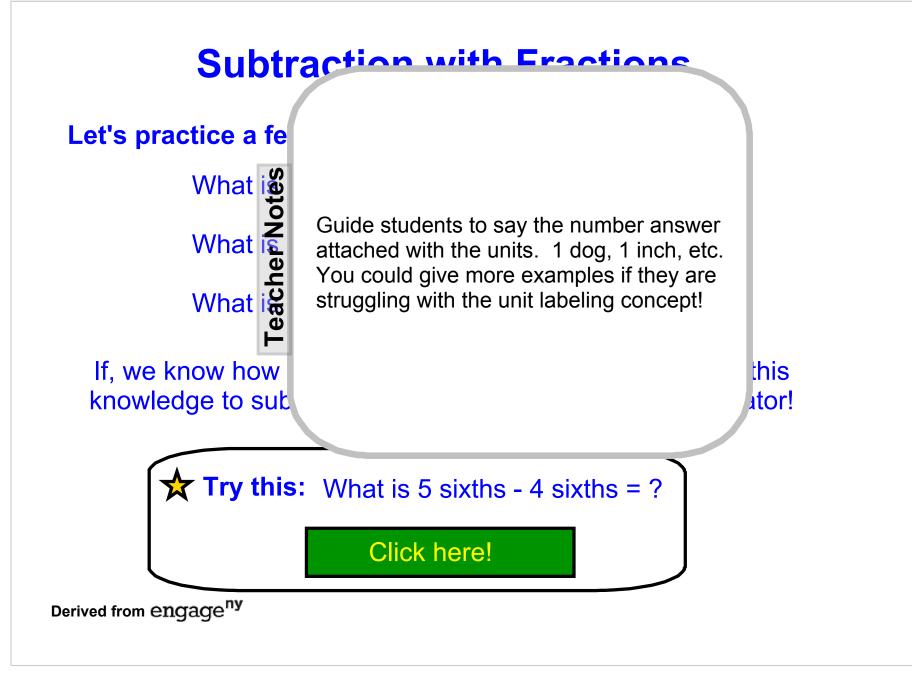
```
What is 5 - 4 = ?
```

What is 5 dogs - 4 dogs = ?

What is 5 inches - 4 inches = ?

If, we know how to subtract whole numbers, we can use this knowledge to subtract fractions with a common denominator!





Subtracting Fractions with Common Denominators

Subtracting fractions with a common denominator is similar to when we added fractions with a common denominator.

Let's Talk:

Think about the problem 5 sixths minus four sixths:

1. What do you think is different when we subtract fractions from when we added fractions?

2. What do you think is the same?



Encourage students to discuss the Con questions about similarities and differences with a partner or small group. You should guide the conversation to recognize that Subtracting fr the denominators stay the same when we add and subtract, but themath function Teacher Teacher Teacher changes (the difference).

ilar to

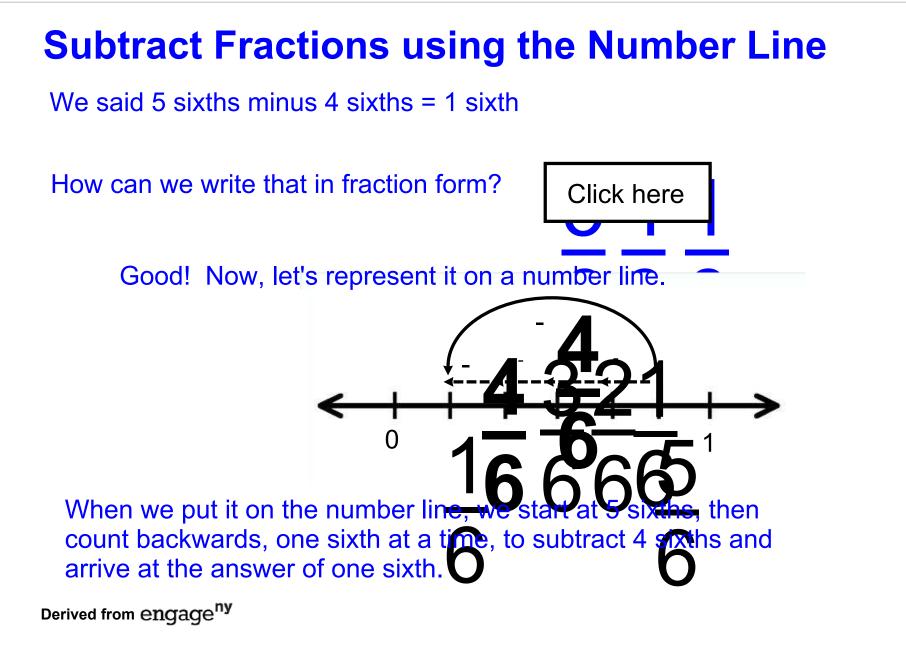
Dr.

The denominator indicates the number of parts of the whole. If the fractions have a common denominator, they are the same "size" so we can subtract the numerators (or number of parts). We are taking away Think about parts instead of adding more. .ns:

1. What do you think is different when we subtract fractions from when we added fractions?

Let's Talk:

2. What do you think is the same?



Subtract Fractions using the Number Line

We said 5 sixths m

How can we write Good! Notes Students should write and draw the depictions of subtracting 5 sixths from 4 sixths. They should be able to compose the fractions in an equation and construct the number line with 6 equal parts independently, but may need some guidance showing how you count backwards 4 sixths. You may need to revisit how each section between "ticks" is worth 1 part of the whole. Make sure students are counting between marks appropriately to account for each part.

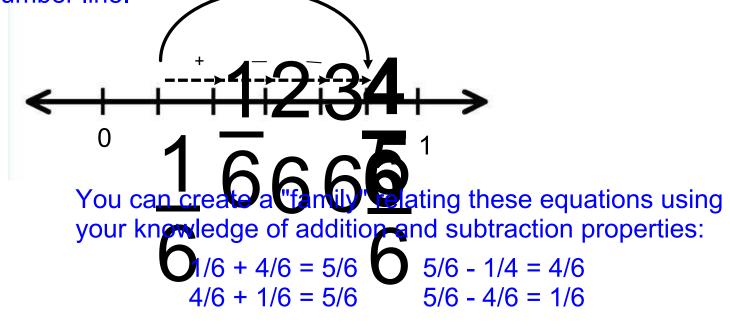
When we put it on the number line, we start at 5 sixths, then count backwards, one sixth at a time, to subtract 4 sixths and arrive at the answer of one sixth.

Derived from engage^{ny}

Subtracting Related to Addition

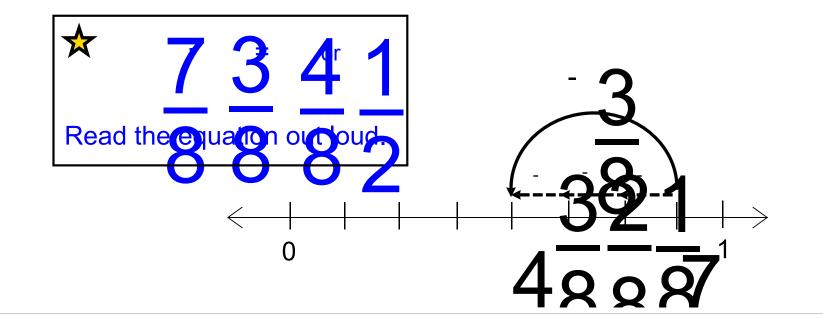
On the previous slide we demonstrated how to use the number line to subtract fractions. Remember, you can use the same process when adding fractions. All of your equations are part of the same family. Let's look at this a little closer.

We know that 5/6 - 4/6 = 1/6. If this is true, then 1/6 + 4/6 should also equal 5/6. Let's show how this is true using a number line.



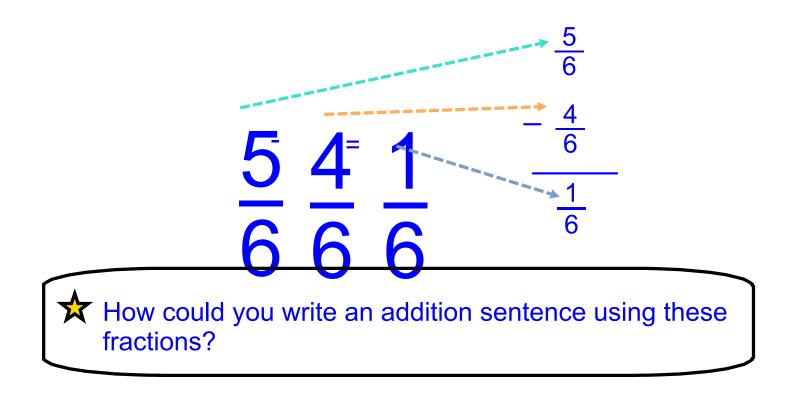


Solve 7 3 and draw a number line to represent this problem. Remember we only subtract the numerators! Leave the denominators the same.

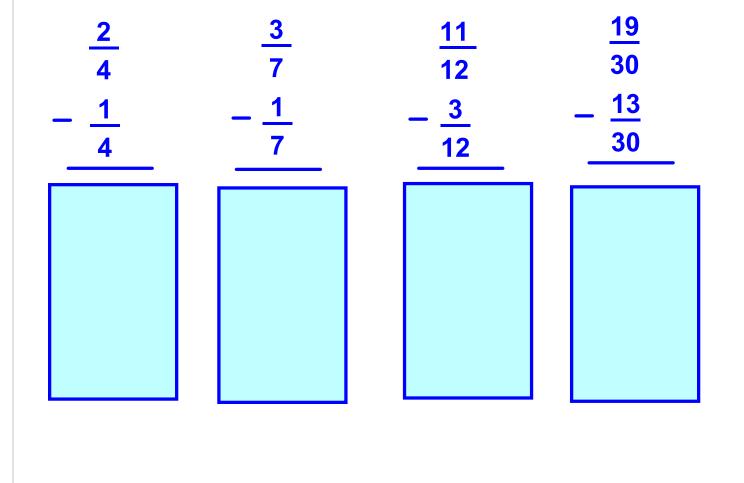


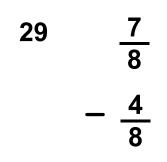
Writing Fractions Vertically

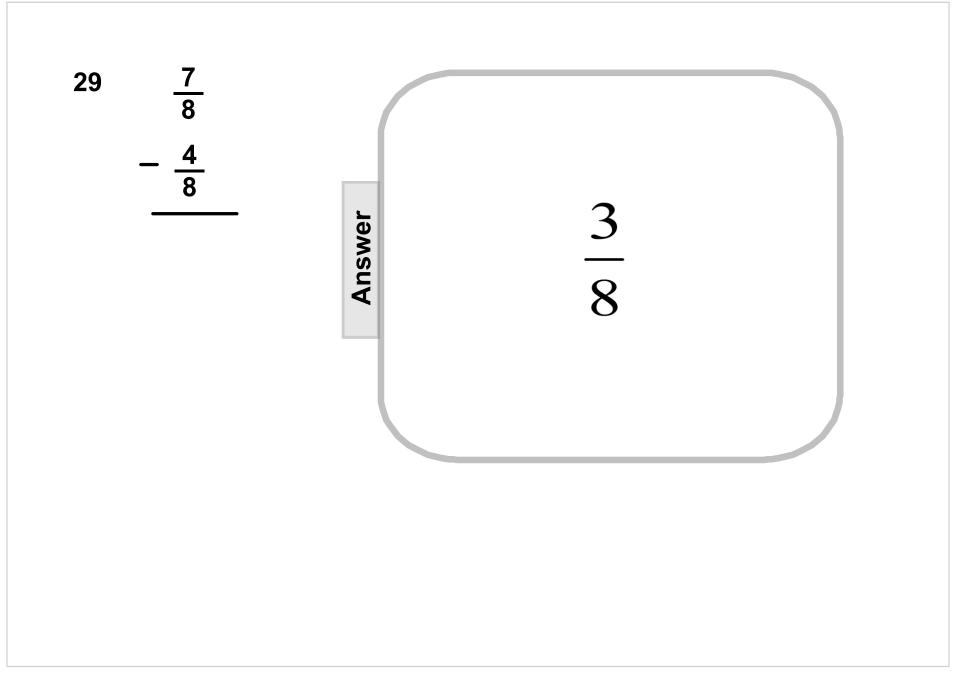
Just like when adding fractions, you can also subtract fractions by writing them vertically. Remember, the denominator indicates the number of parts of the whole. If the fractions have a common denominator, they are the same "size" so we can subtract the numerators (or number of parts).

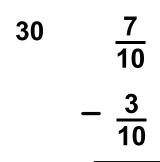


Try these! Click the boxes to see work and answers. Be sure to simplify all answers.

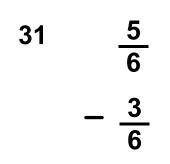


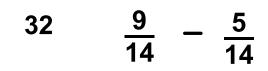




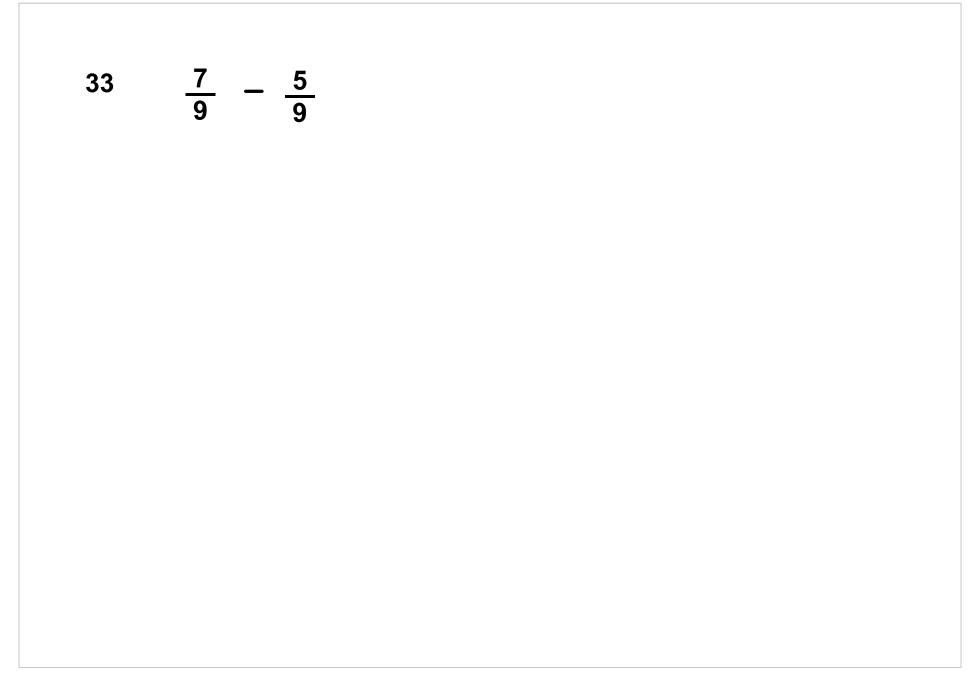


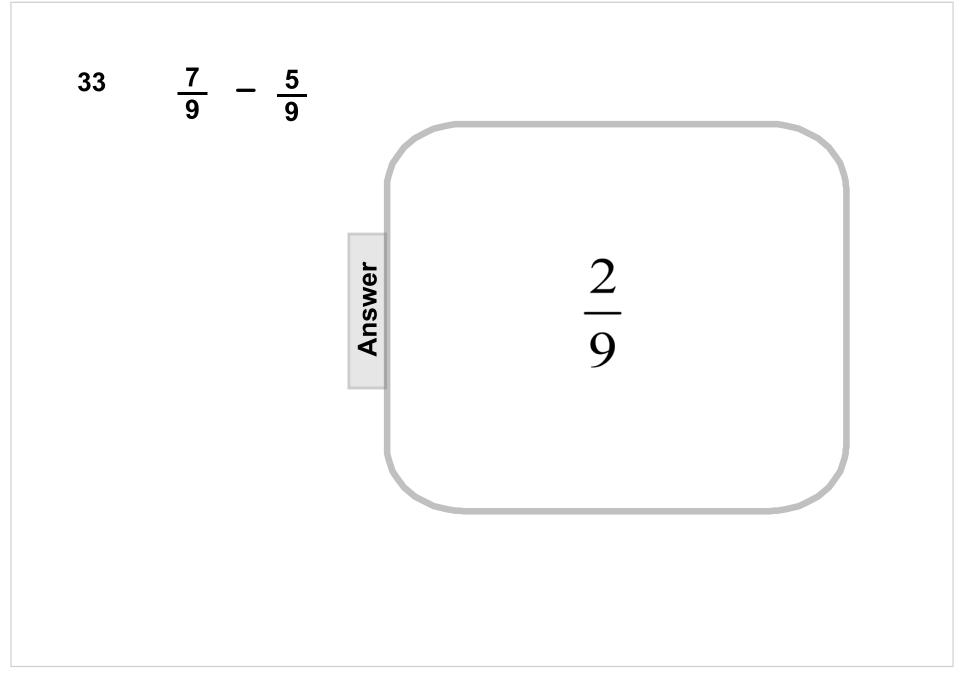
Slide 70 (Answer) / 110





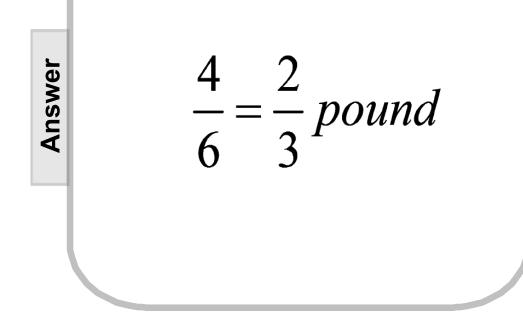
Slide 72 (Answer) / 110





34 Joel made a batch of fresh cookies with 5/6 of a pound of butter and 1/6 of a pound of sugar. How much more butter than sugar was used?

34 Joel made a batch of fresh cookies with 5/6 of a pound of butter and 1/6 of a pound of sugar. How much more butter th



35 The pizza place puts three-fourths of a cup of sauce on a large pizza and one-fourth of a cup of sauce on a personal pizza. How much more sauce is on a large pizza? 35 The pizza place puts three-fourths of a cup of sauce on a large pizza and one-fourth of a cup of sauce on a personal pizza. How much more sauce is on a large r

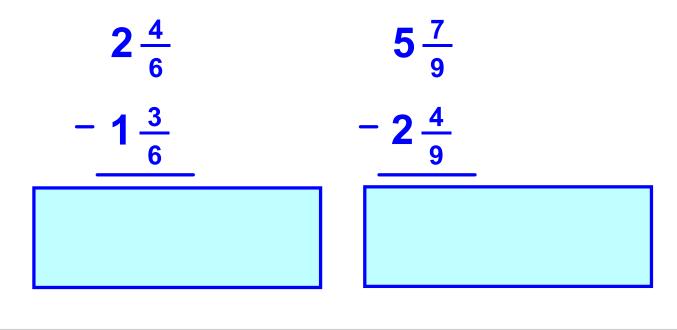
 $\frac{2}{4} = \frac{1}{2}cup$

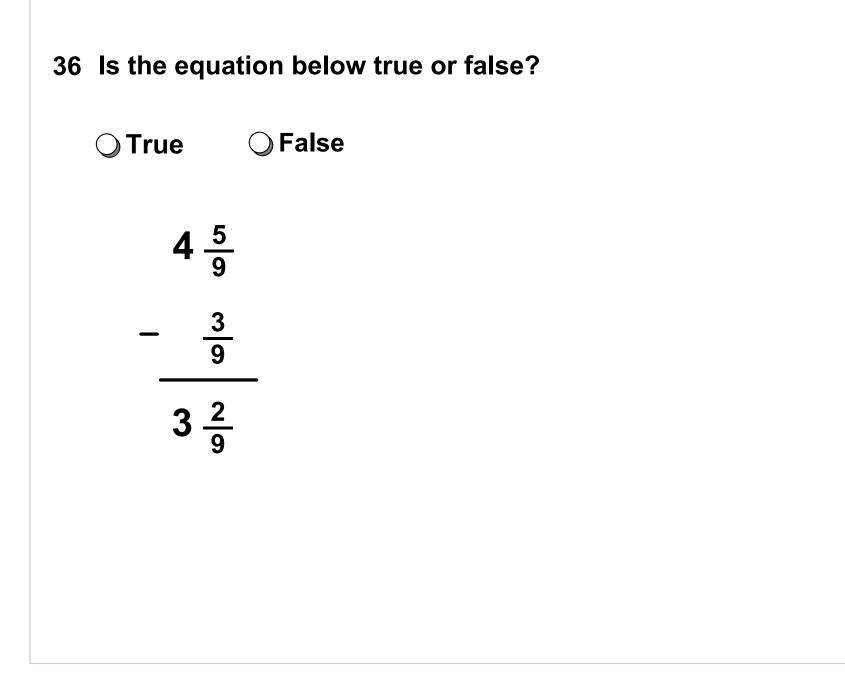
Subtracting Mixed Numbers with Common Denominators

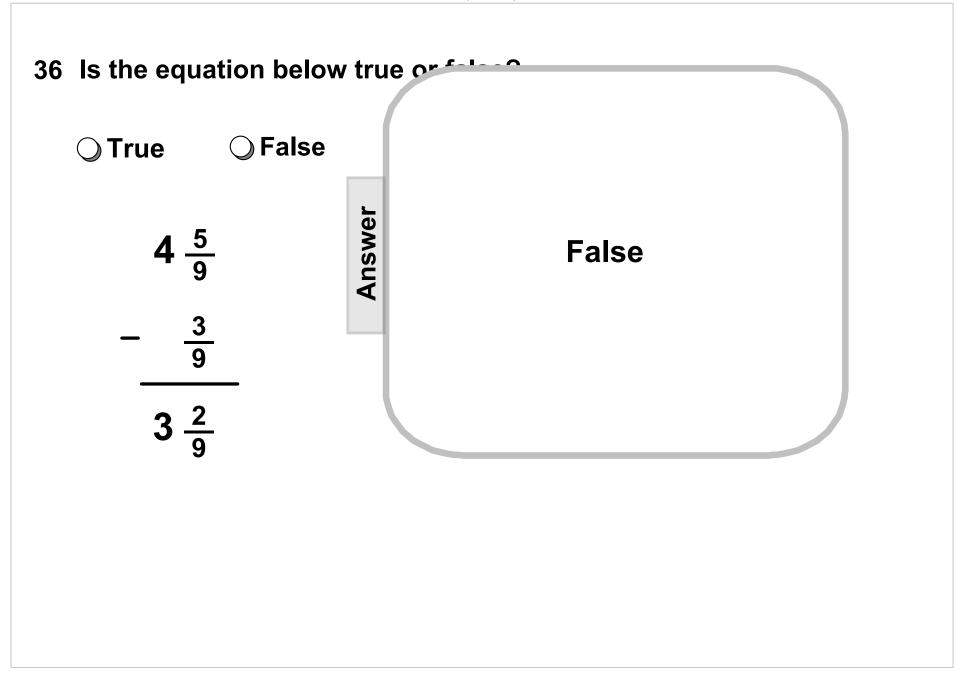
> Return to Table of Contents

Subtracting Mixed Numbers with Common Denominators

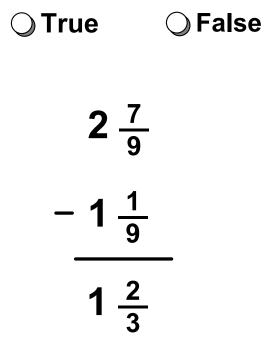
To subtract mixed numbers with common denominators, subtract the fractions then subtract the whole numbers. Make sure your answer is in simplest form.

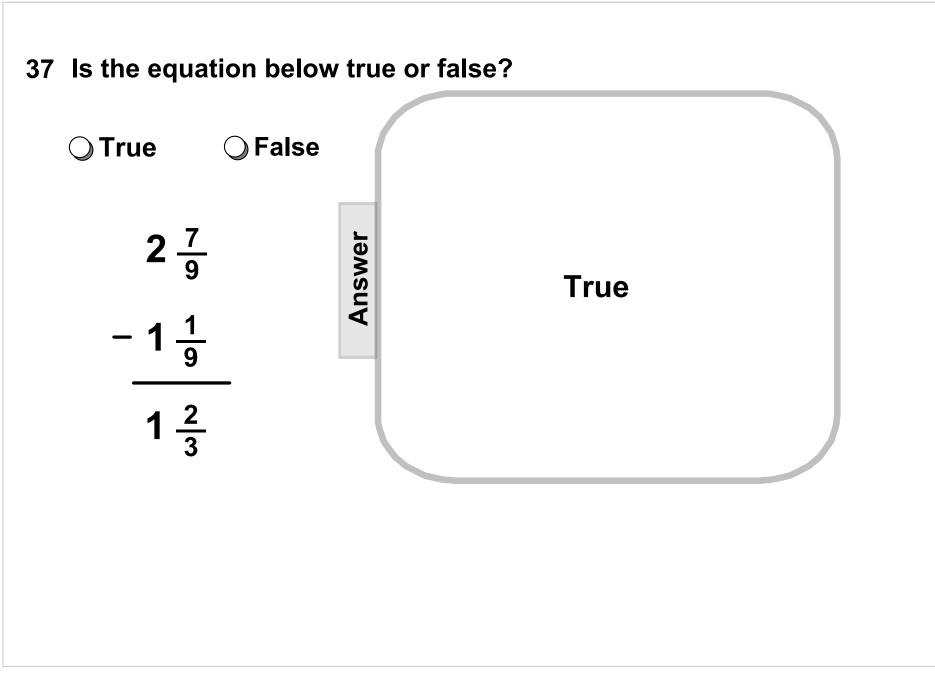




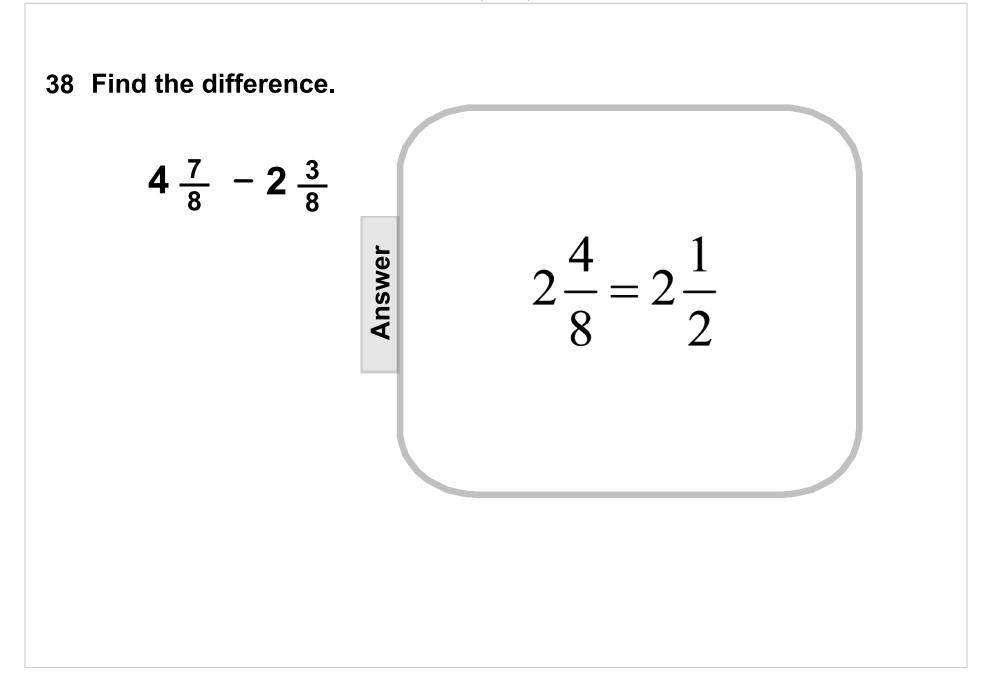




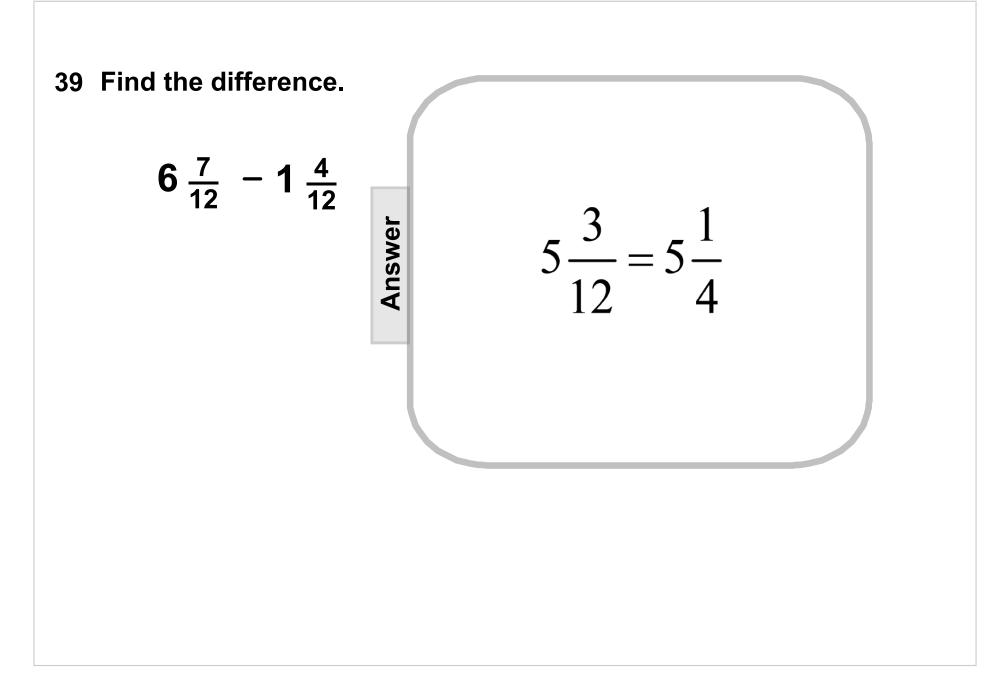




$$4\frac{7}{8} - 2\frac{3}{8}$$

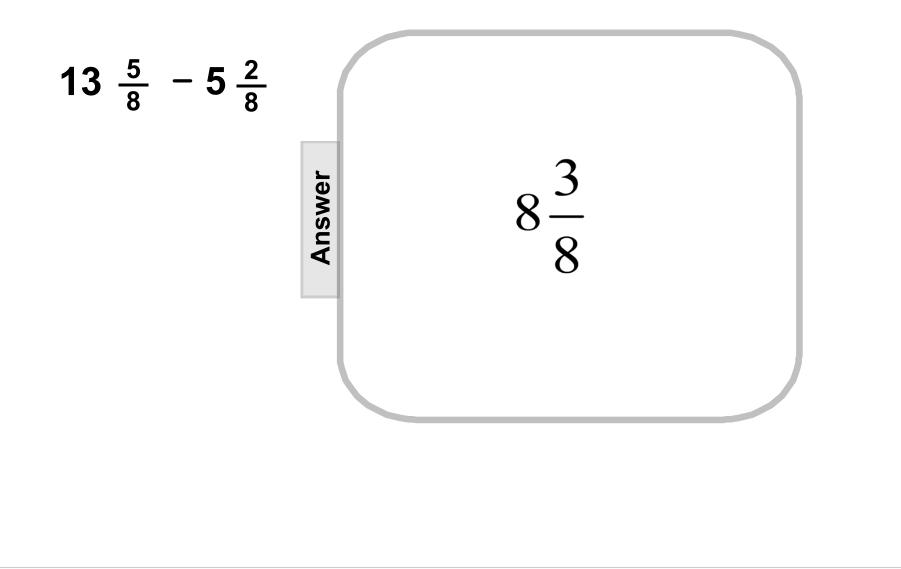


$$6\frac{7}{12} - 1\frac{4}{12}$$



$$13 \frac{5}{8} - 5 \frac{2}{8}$$





41 How many inches more of rain was there in January than March?

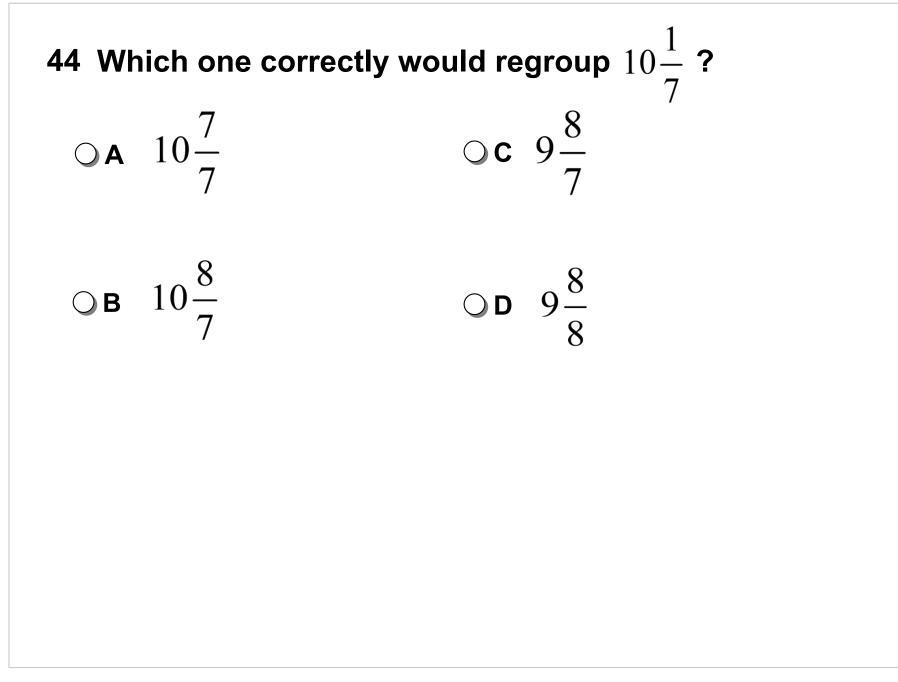
Month	Inches of Precipitation
January	$12\frac{5}{6}$
February	$8\frac{4}{6}$
March	$2\frac{1}{6}$
April	$9\frac{2}{6}$
Мау	$1\frac{1}{6}$

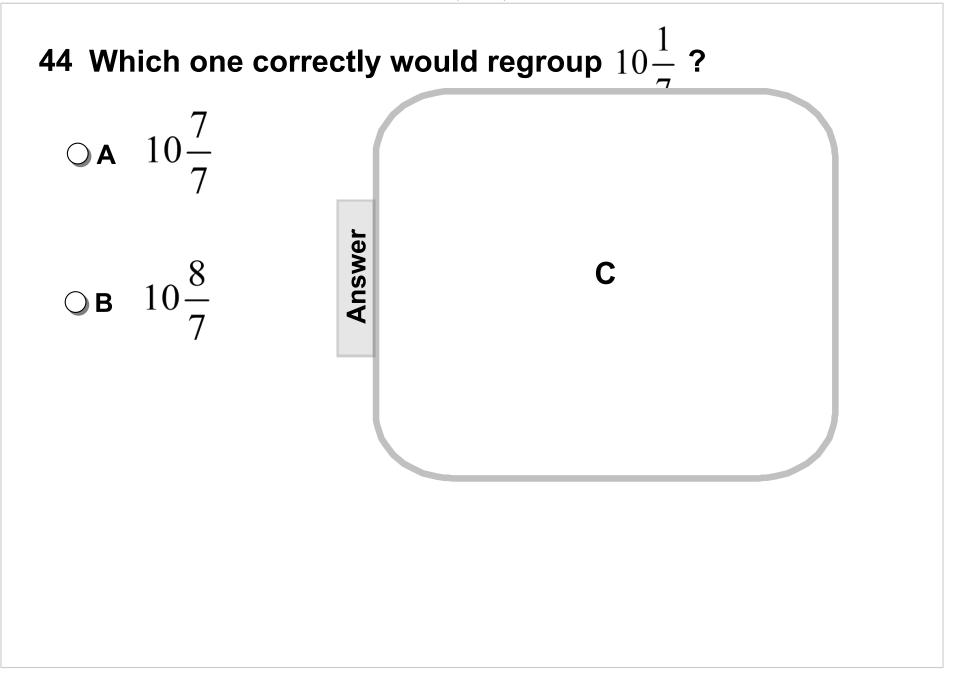
42 How many inches more of rain was there in April than May?

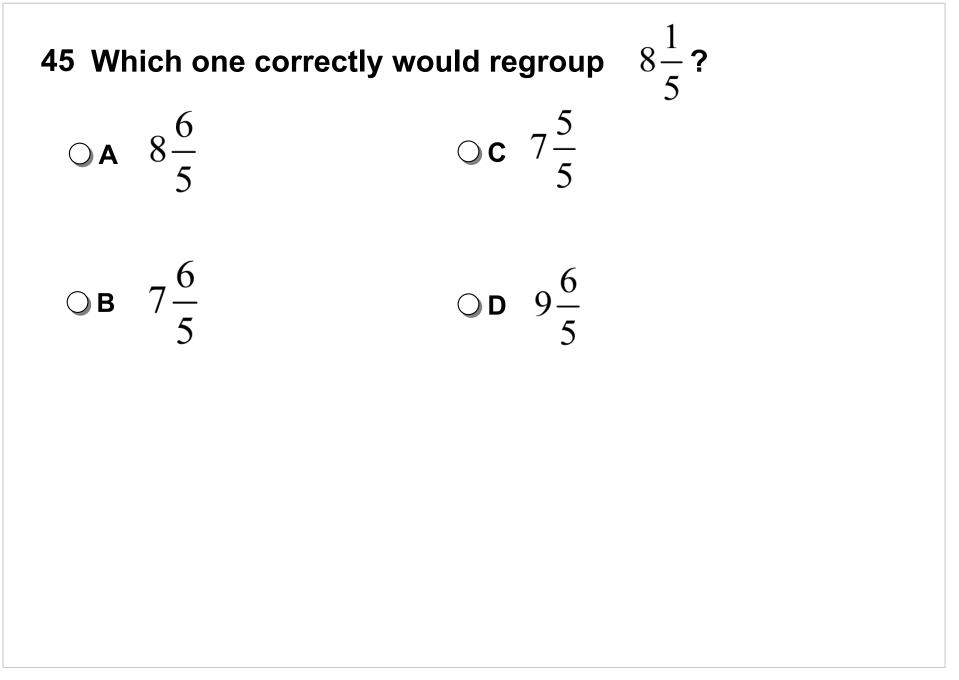
Month	Inches of Precipitation
January	$12\frac{5}{6}$
February	$8\frac{4}{6}$
March	$2\frac{1}{6}$
April	$9\frac{2}{6}$
Мау	$1\frac{1}{6}$

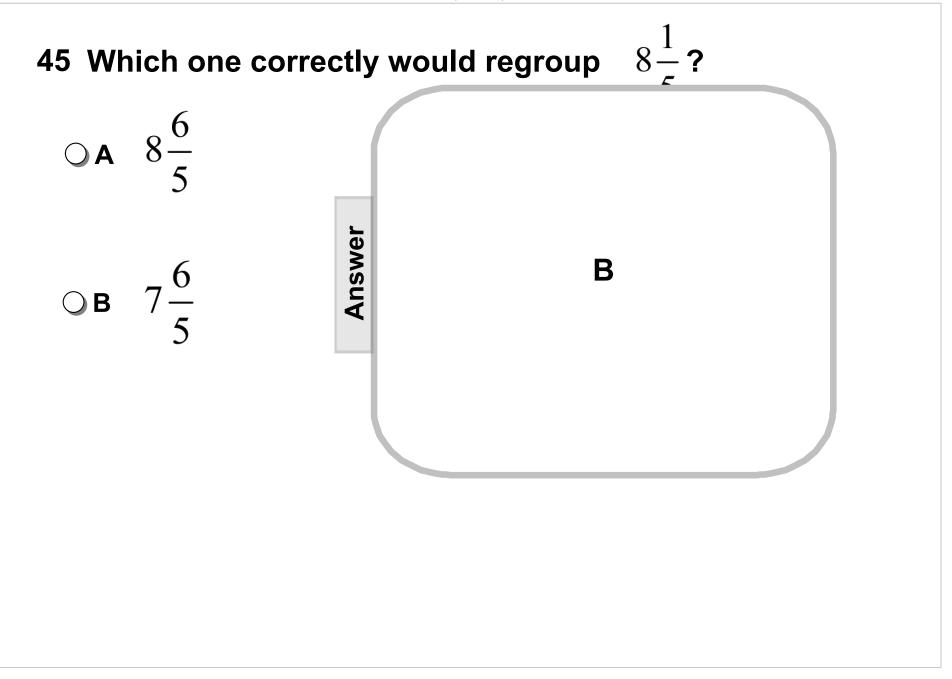
43 How many inches more of rain was there in February than March?

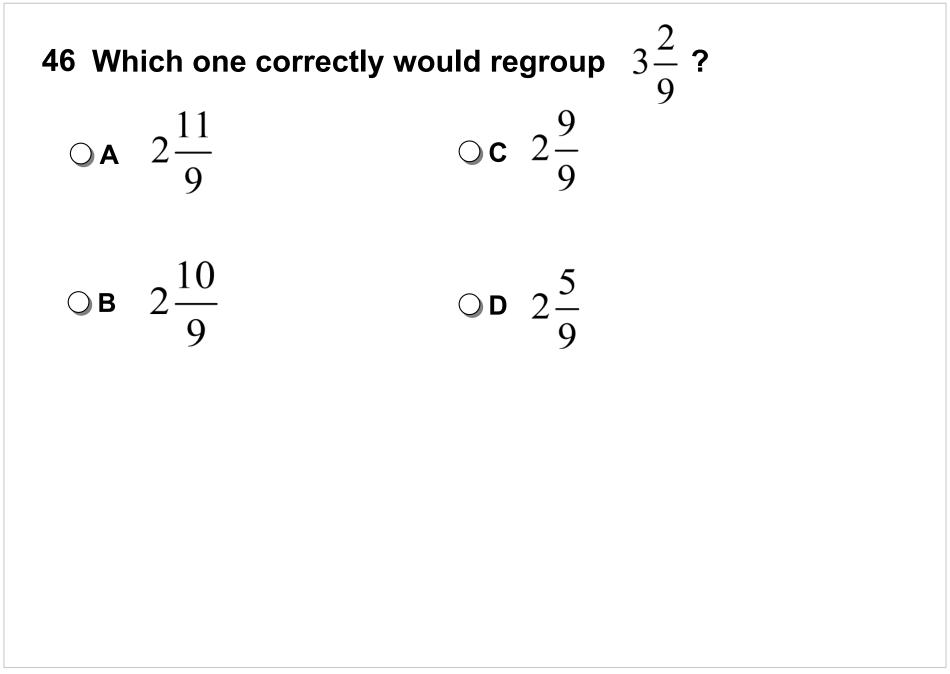
Month	Inches of Precipitation
January	$12\frac{5}{6}$
February	$8\frac{4}{6}$
March	$2\frac{1}{6}$
April	$9\frac{2}{6}$
Мау	$1\frac{1}{6}$

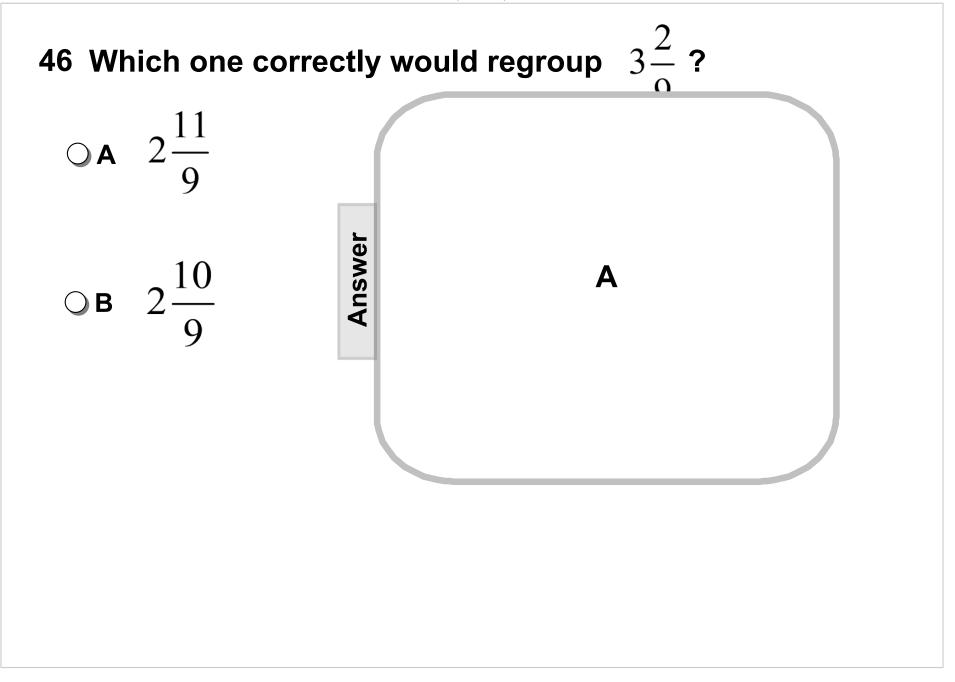




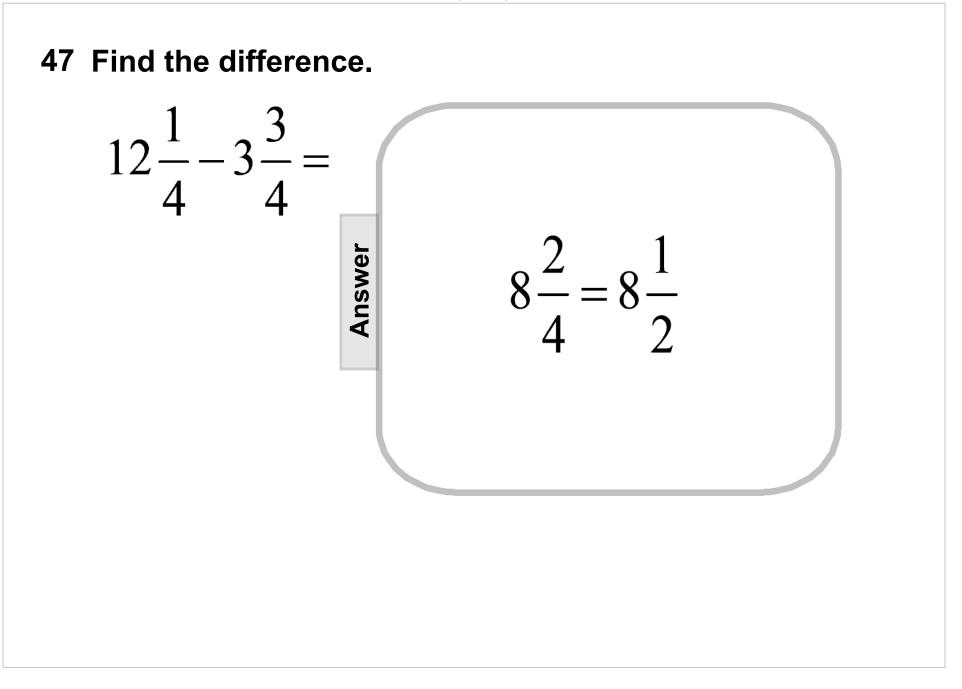




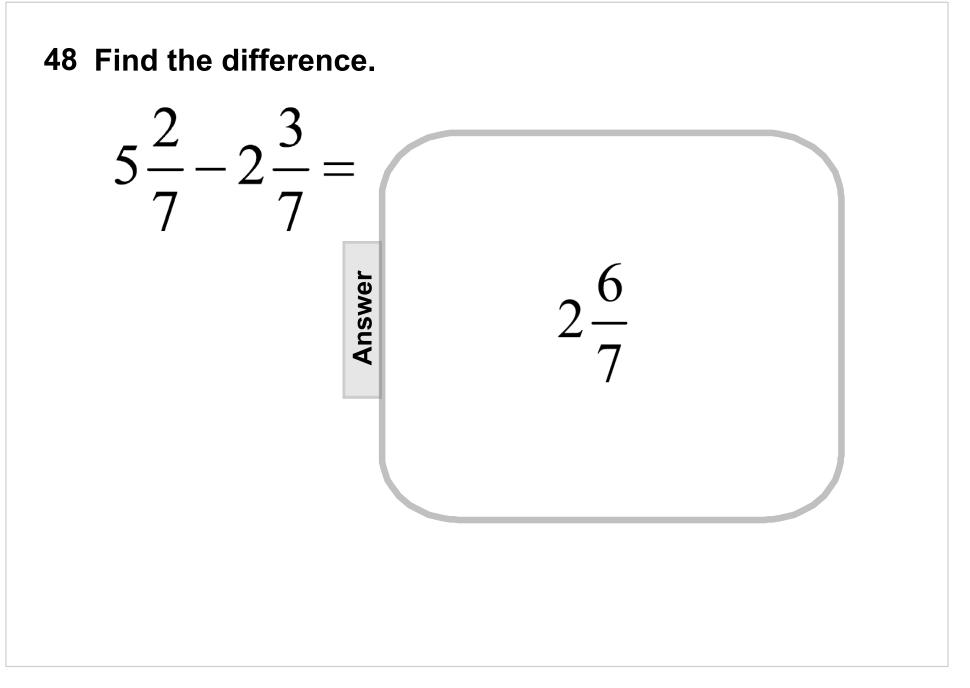




 $12\frac{1}{4} - 3\frac{3}{4} =$



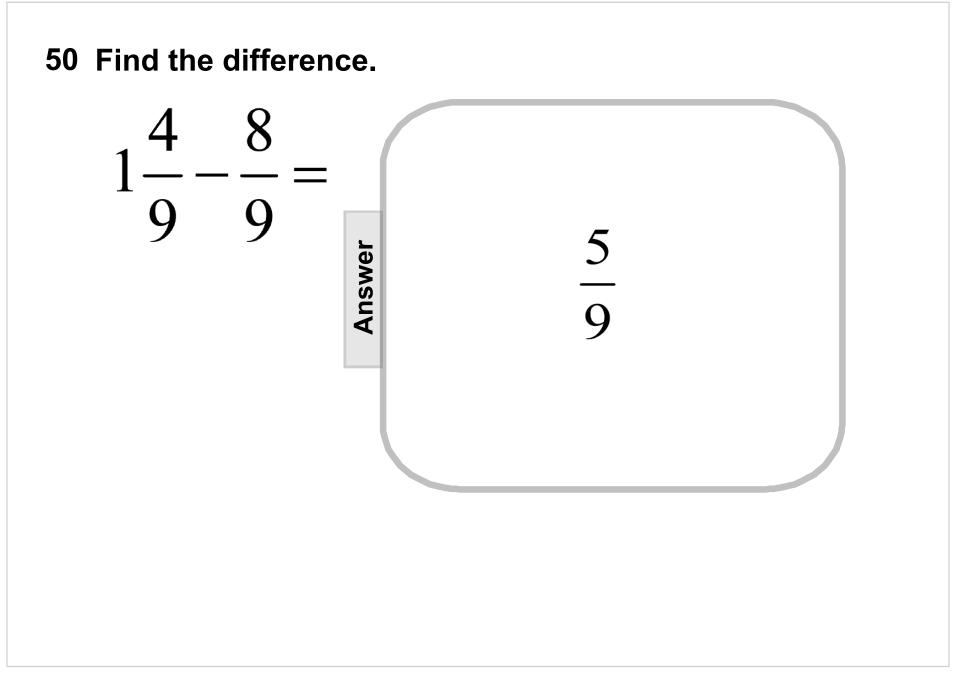
 $5\frac{2}{7}-2\frac{3}{7}=$



Slide 94 (Answer) / 110

50 Find the difference.

8 9 9



51 Victoria's hair is twenty two and three-eighths inches long. Miranda's hair is nine and five-eighths inches long. How much longer is Victoria's hair than Miranda's hair? 51 Victoria's hair is twenty two and three-eighths inches long. Miranda's hair is nine and five-eighths inches long. How much hair than Miranda's /

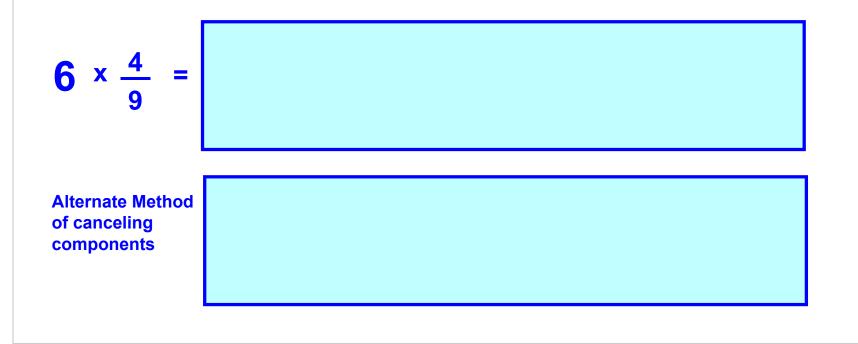
Answer

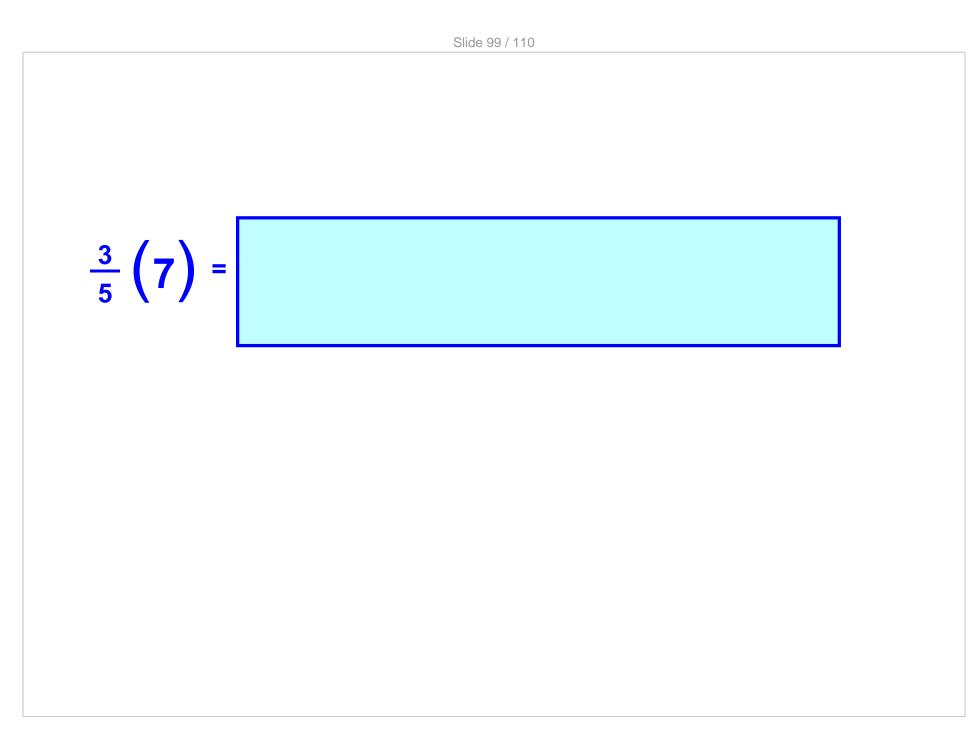
 $12\frac{6}{8} = 12\frac{3}{4}$

Multiplying Fractions and Whole Numbers

Return to Table of Contents To multiply fractions with whole numbers, write the whole number as a fraction (over 1) then multiply the two fractions.

Make sure you write your answer in simplest form.



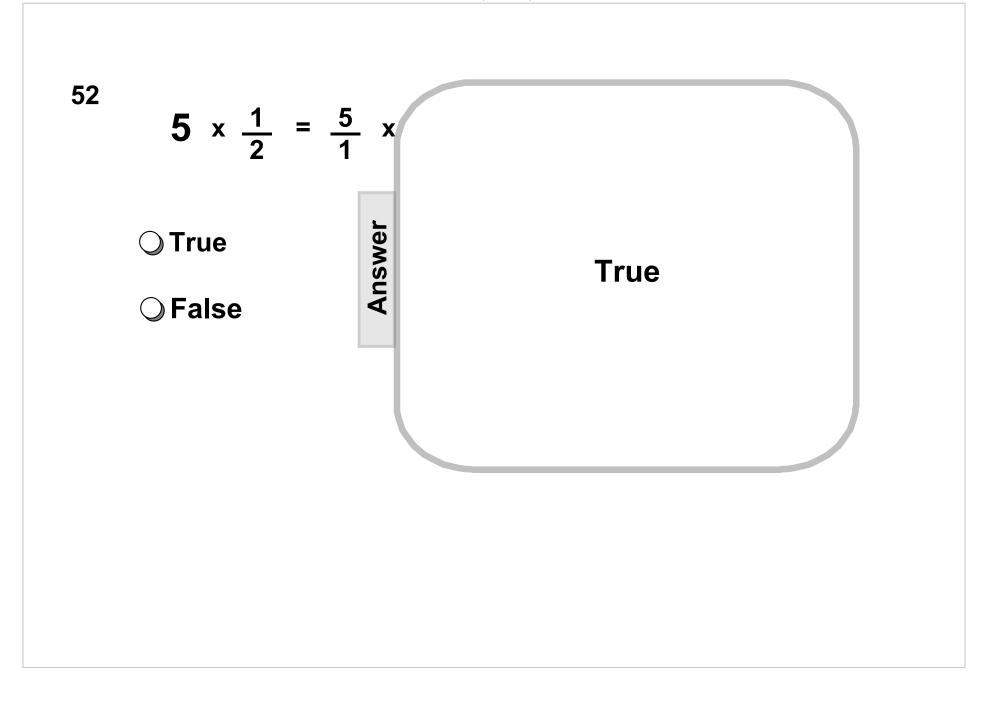


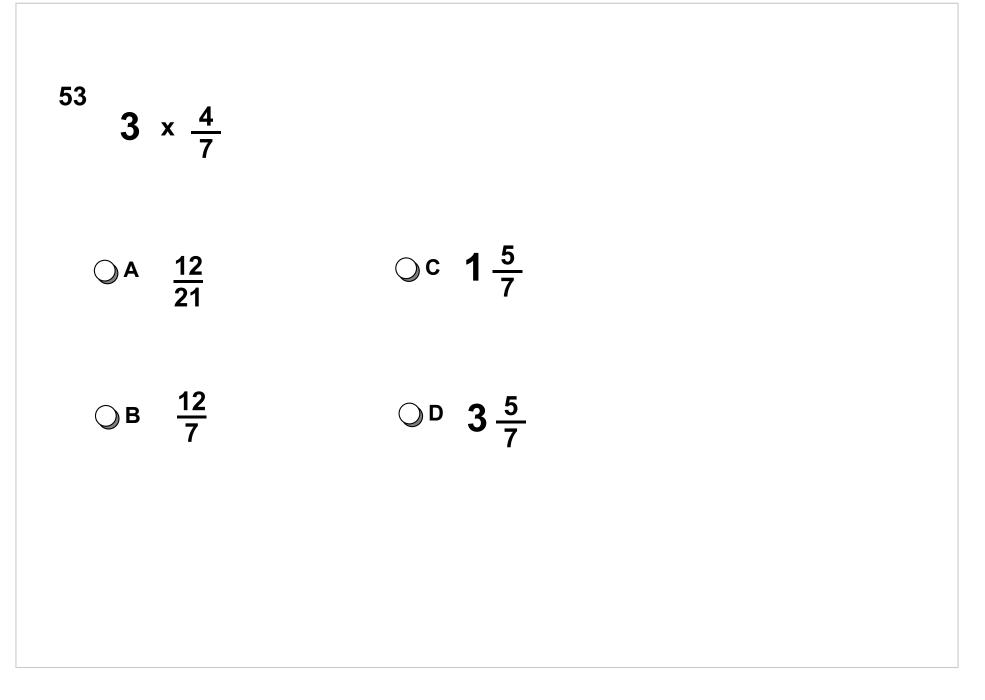
52

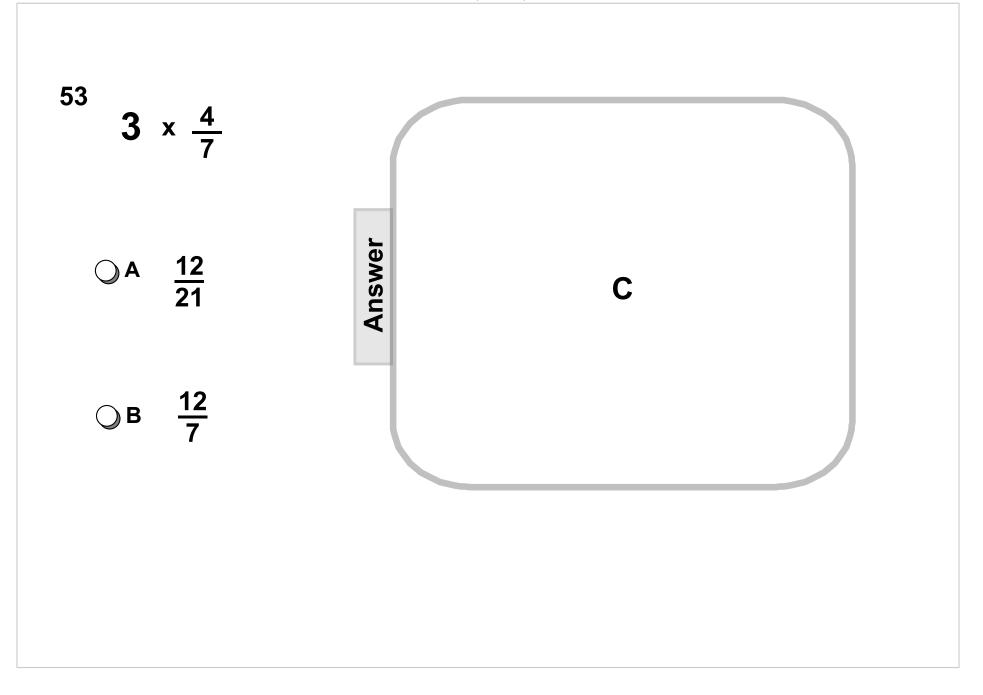
$$5 \times \frac{1}{2} = \frac{5}{1} \times \frac{1}{2}$$

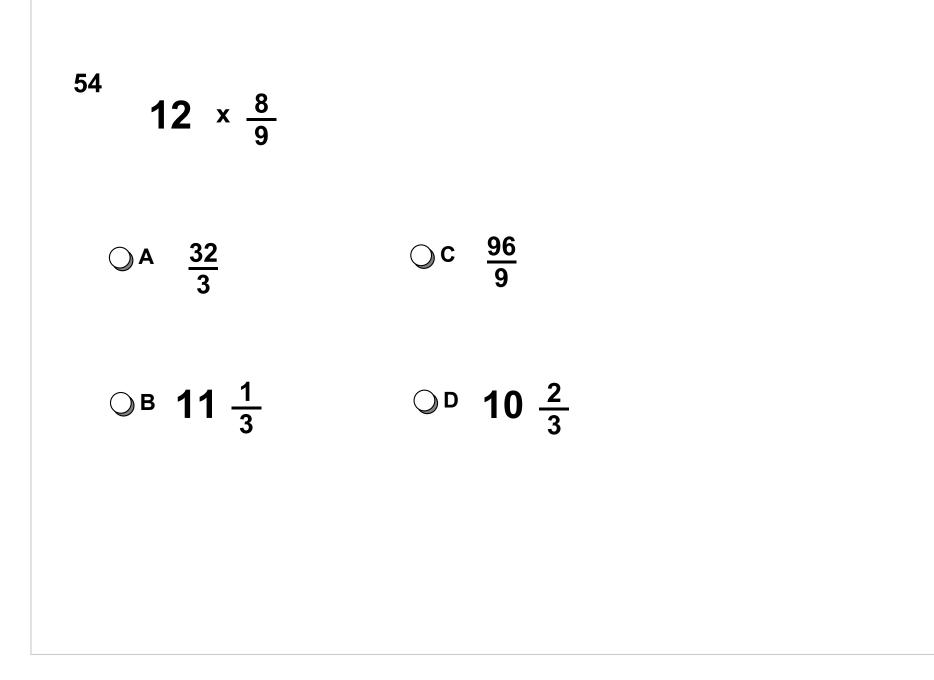
\bigcirc True

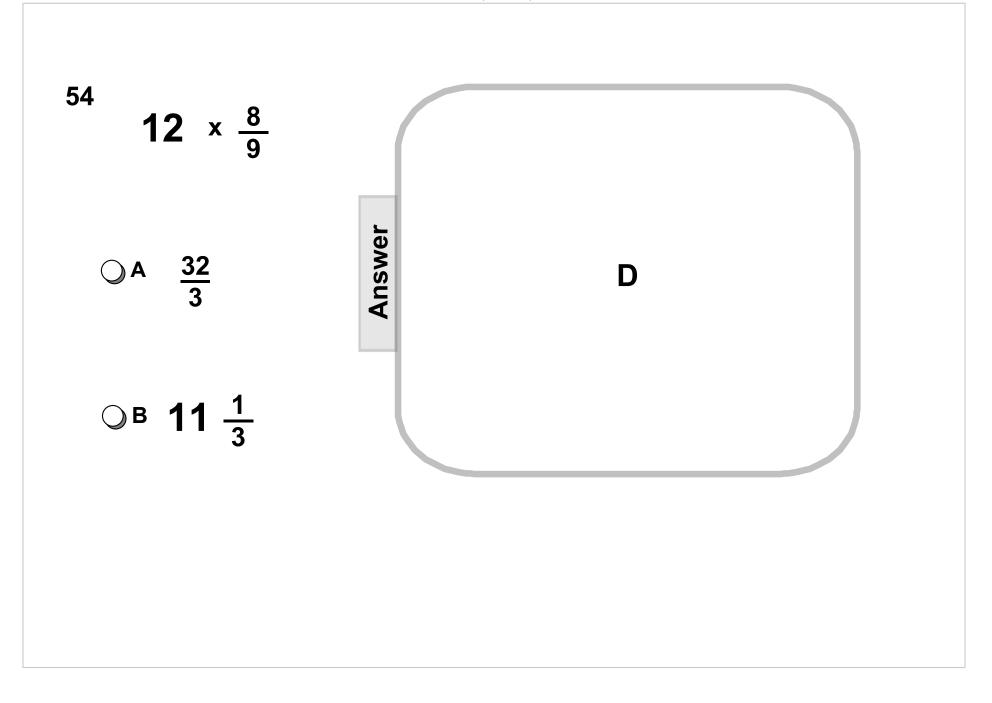
 \bigcirc False

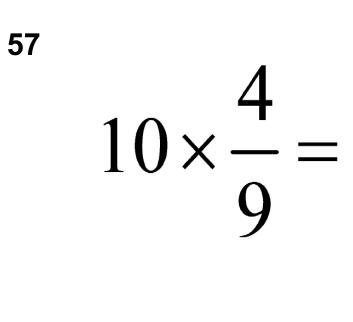


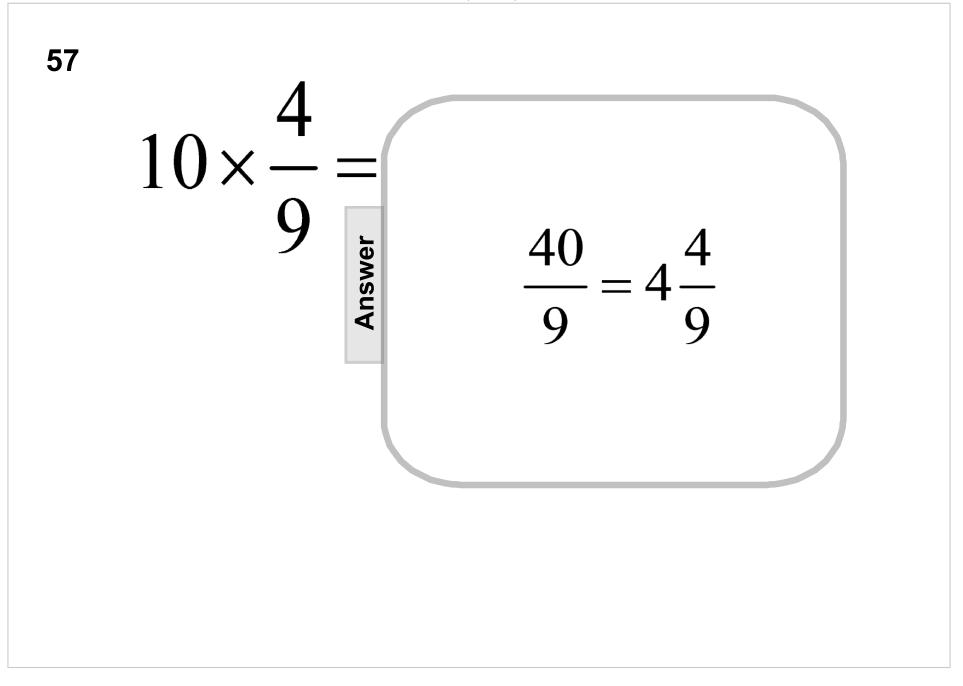






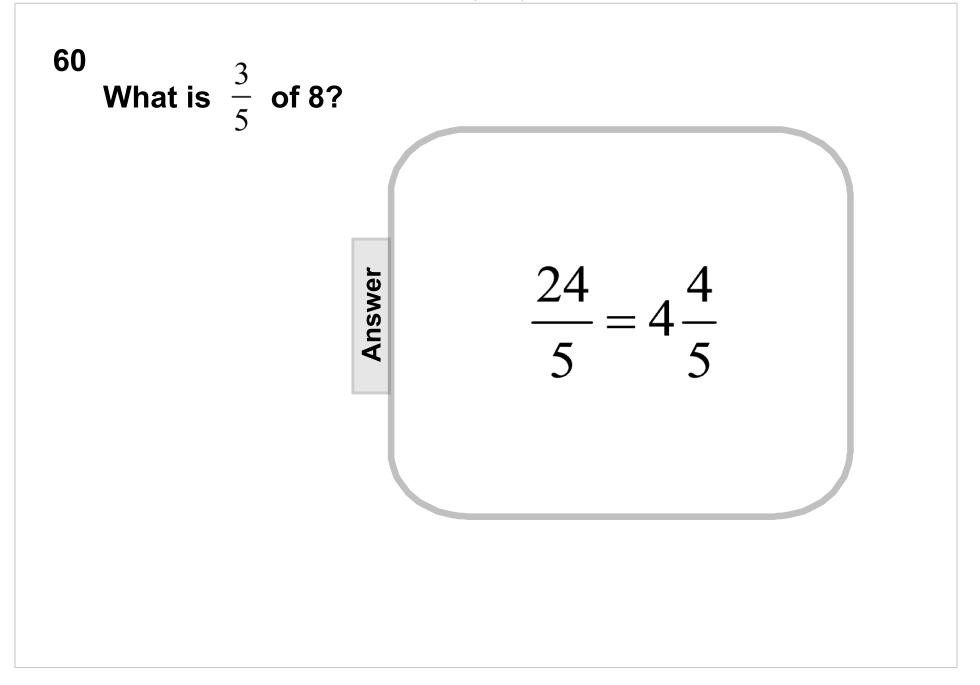






59 What is $\frac{7}{9}$ of 12?

60 What is $\frac{3}{5}$ of 8?



61 What is $\frac{4}{9}$ of 9?

62 What is $\frac{2}{3}$ of 7?

